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A cartoon illustration of a brown owl with large white eyes, wearing a white graduation cap with a blue tassel. The owl is standing on a dark silhouette of a tree branch against a dark blue background.

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The AISC logo is a circular seal with "AMERICAN INSTITUTE OF STEEL CONSTRUCTION" around the top edge and "FOUNDED 1921" around the bottom edge. In the center, the letters "AISC" are prominently displayed.

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Session Description

Session 2: Design of Vertically Curved Members **June 25, 2018**

This session first addresses general design considerations including architecturally exposed structural steel, tolerances and contract documents. The presentation then addresses the treatment vertically-curved members. Topics include axial strength, flexural strength, combined axial and flexural loads, local strength and connections.



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Learning Objectives

- Identify the 5 categories of Architecturally Exposed Structural Steel (AESS) stated in the 2016 AISC Code of Standard Practice.
- Identify the tolerances for curved steel members stated in the 2016 AISC Code of Standard Practice.
- Describe the design considerations for axial strength of vertically-curved members in terms of in-plane and out-of-plane strength.
- Describe the design considerations for flexural strength of vertically-curved members.



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Design of Curved Members

Session 2: Design of Vertically Curved Members

June 25, 2018



Presented by
Bo Dowswell, P.E., Ph.D.
ARC International, LLC
Birmingham, AL

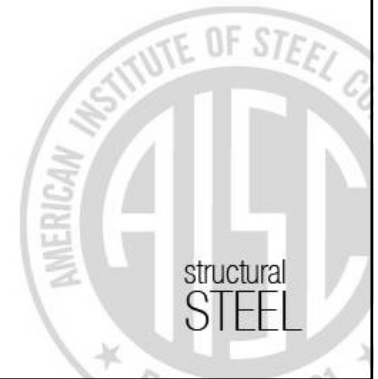
There's always a solution in steel.



There's always a solution in steel.

General Information on Curved Members

Session Description



Session Description

- General Design Considerations
 - Architecturally exposed members
 - Tolerances
 - Contract documents



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Design of Vertically-Curved Members

Session Description



Session Description

- Vertically-curved members
 - Axial strength
 - Flexural strength
 - Combined loads(continued)



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Session Description

- Structural analysis
- Local strength
- Connections



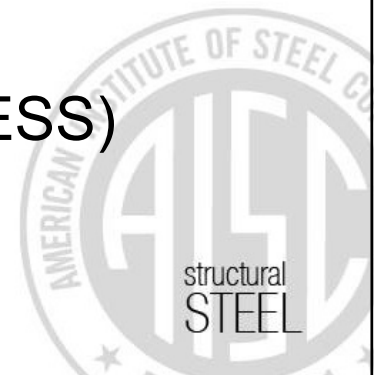
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General Information on Curved Members

General Design Considerations

Architecturally Exposed (AESS)
Members

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AESS Members

2016 AISC Code of Standard Practice (COSP)

- AISC Code of Standard Practice Section 10.1.1 defines five categories of AESS:
 - AESS 1: Basic elements
 - AESS 2: Feature elements viewed at > 20 ft
- (continued)



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AESS Members

- AESS 3: Feature elements viewed at < 20 ft
- AESS 4: Showcase elements
- AESS C: Custom elements

The 2016 COSP is available for free download at:

<https://www.aisc.org/globalassets/aisc/publications/standards/code-of-standard-practice-june-15-2016.pdf>



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AESS Members

- For further information on AESS, see the Nov. 2017 issue of *Modern Steel Construction*:
https://www.aisc.org/globalassets/aisc/aess/all_about_aess_reprint.pdf
 - Generally, the bending cost increases with increasing AESS category
-



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AESS Members

- Generally, the bending cost increases with increasing AESS category
-



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There's always a solution in steel.

General Information on Curved Members

General Design Considerations

Tolerances



Tolerances

2016 AISC *Code of Standard Practice (COSP)*

- Chord length tolerance
- Curvature tolerance
- Similar to those for straight members
- Tolerances for AESS are the same as non-AESS



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Tolerances

2016 AISC Code of Standard Practice (COSP)

- No cross-sectional distortion tolerance
- Tolerances that are not addressed in the COSP should be mutually agreed upon by the contractor and the owner

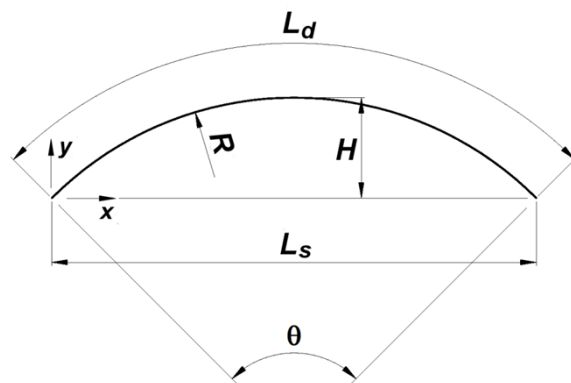


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Tolerances

Chord Length Tolerance

- Tolerance on L_s
- COSP Section 6.4.2(b)

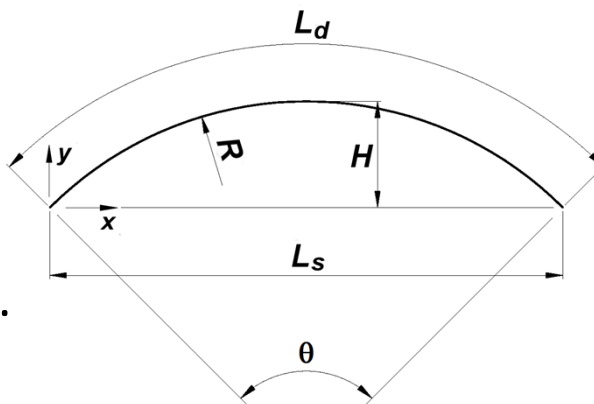


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Tolerances

Chord Length Tolerance

- Members that frame to other structural steel elements:
 - For $L_s \leq 30$ ft: $\pm 1/16$ in.
 - For $L_s > 30$ ft: $\pm 1/8$ in.

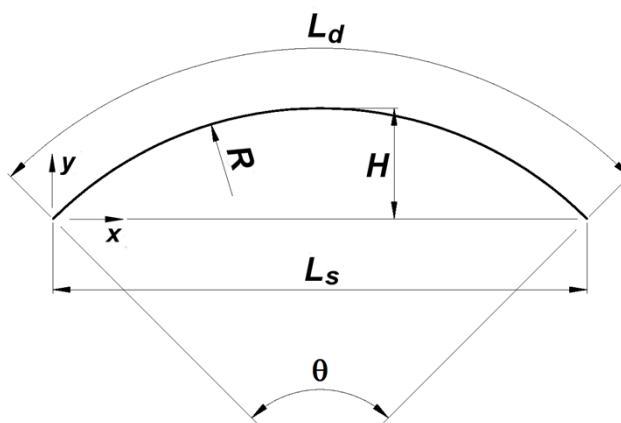


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Tolerances

Curvature Tolerance

- Tolerance on H
- Non-AESS: COSP
Section 6.4.2(b)
- AESS: COSP
Section 10.4.4

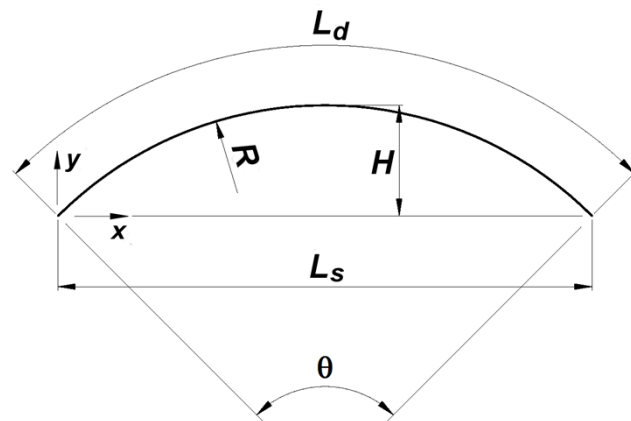


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Tolerances

Curvature Tolerance

- Dependent on L_d



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Tolerances

Curvature Tolerance

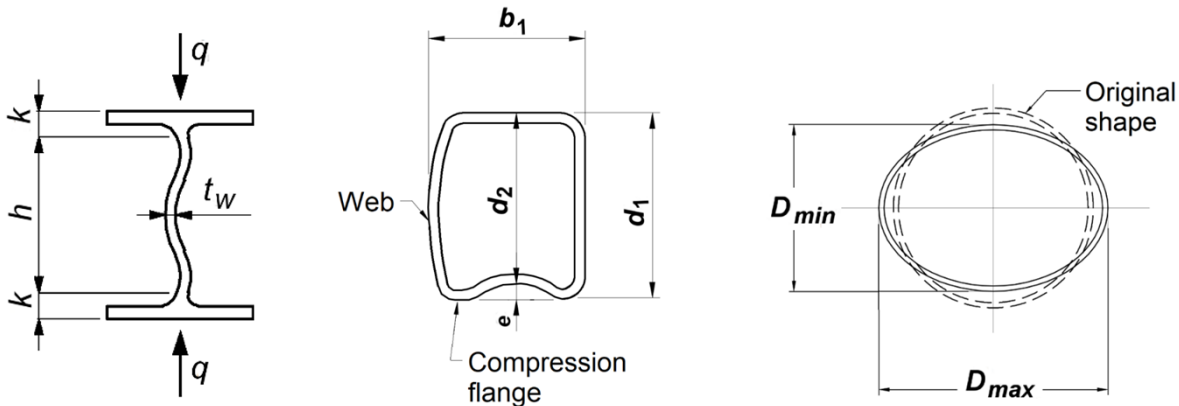
- Equal to the camber and sweep tolerances for straight members in the applicable ASTM standard
- Sharp kinks or sharp bends are cause for rejection



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Tolerances

Distortion Tolerance



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Tolerances

Distortion Tolerance

- Should be based on:
 - The potential effect on structural performance
 - Any aesthetic requirements for AESS members
- Should be established with input from the bender/roller



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Tolerances

Distortion Tolerance: Structural Effects

- Reasonable cross-sectional distortions can be tolerated without a reduction in strength
- See Design Guide Section 5.5 for further information



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Tolerances

Distortion Tolerance: AESS

- Generally, AESS requirements are more stringent than strength requirements
- Members with large- and medium-radius bends are likely to be acceptable for AESS 1 and 2 without further consideration



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Tolerances

Distortion Tolerance

- Cross-sectional tolerances specified in ASTM A6, ASTM A53 and ASTM A500 are mill tolerances
- Initial geometric imperfections are amplified during the bending process



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Tolerances

Distortion Tolerance: Rectangular HSS

- The permissible cross-sectional variation for ASTM A500 rectangular HSS members larger than 5½ in. is 1% of the largest outside flat dimension

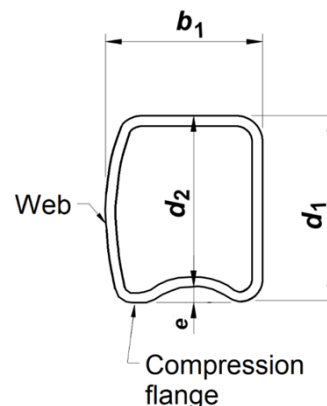


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Tolerances

Distortion Tolerance: Rectangular HSS

- Post-bending wall flatness tolerances (ρ_w and ρ_f) between 1% and 2% are common

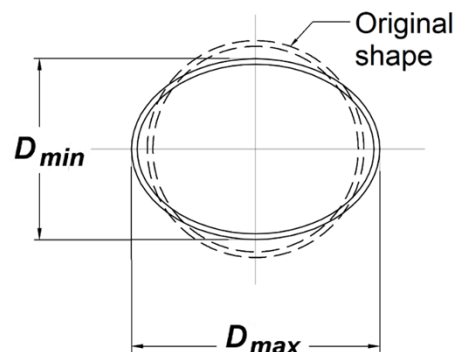


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Tolerances

Distortion Tolerance: Round HSS

- A post-bending ovality tolerance (ρ) of 5% is common



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Tolerances

Distortion Tolerance: Round HSS

- Practical considerations may dictate more stringent tolerances

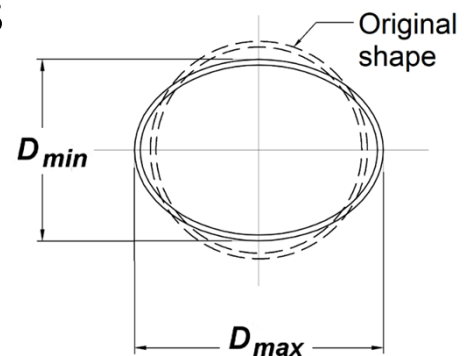


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Tolerances

Distortion Tolerance: Round HSS

- Example: when two segments are connected with circumferential butt welds, proper wall alignment is essential



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Tolerances

Distortion Tolerance: Round HSS

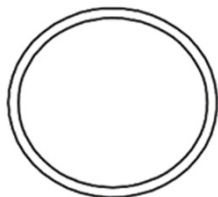
- For AESS, a 5% tolerance is likely to produce imperceptible ovalization distortions



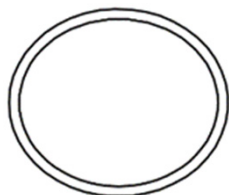
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Tolerances

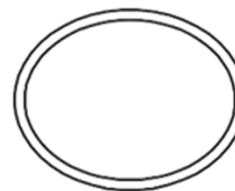
Distortion Tolerance: Round HSS



$\rho = 5\%$



$\rho = 8\%$



$\rho = 12\%$



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General Information on Curved Members

General Design Considerations

Contract Documents



Contract Documents

Member Sizes

- Often controlled by bending requirements rather than performance under service loads
- Member sizes shown on the design drawings should consider bending requirements



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Contract Documents

Architecturally Exposed (AESS) Members

- All AESS members must be identified in the contract documents
- AESS members must be assigned a category defined in *AISC Code of Standard Practice* Section 10.1.1



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Contract Documents

Distortion Tolerances

- Distortion tolerances should be specified in the contract documents



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Design of Vertically-Curved Members

Axial Strength



Axial Strength

Arches

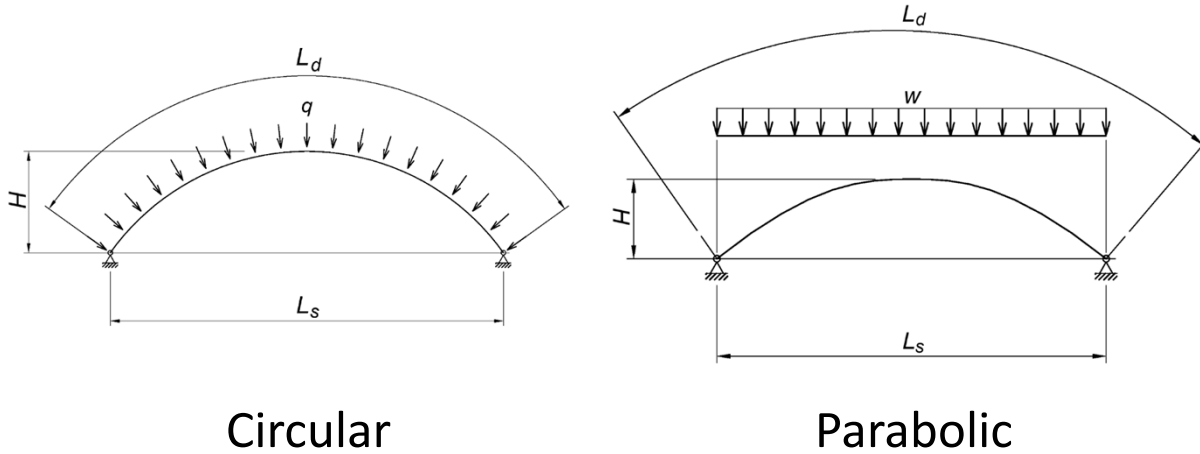
- Structurally efficient
- Loads carried primarily by compression



Photograph courtesy of the AISC Bender/Roller Committee

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Axial Strength



Design of Vertically-Curved Members

Axial Strength

In-Plane Strength

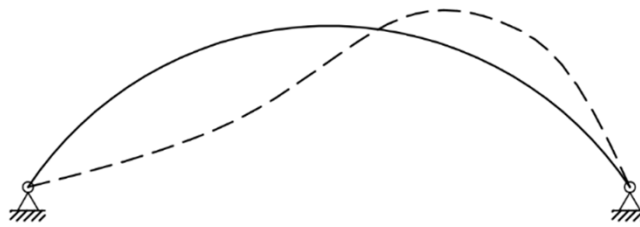


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In-Plane Strength

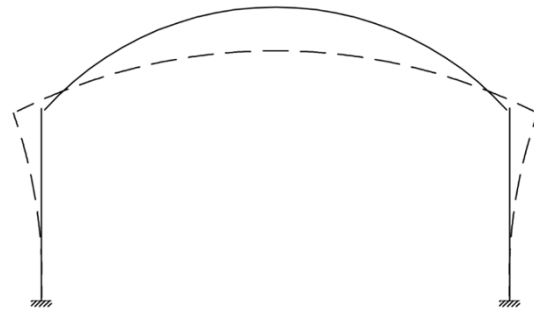
- Curved Members \neq Straight Members
- Buckled Shape



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In-Plane Strength

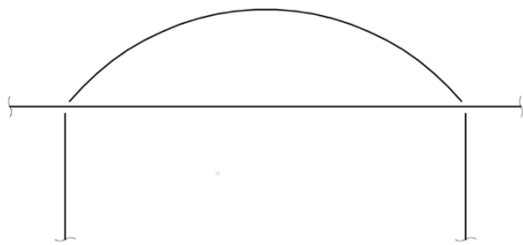
- Support spreading
 - Increases deflection
 - Can lead to collapse



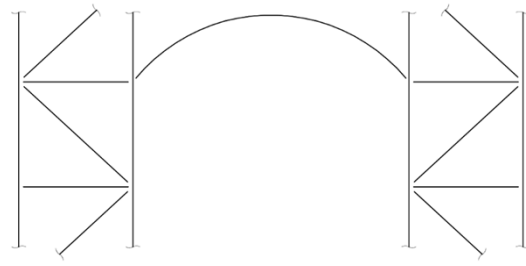
48

In-Plane Strength

- Horizontal restraints



Tension Tie

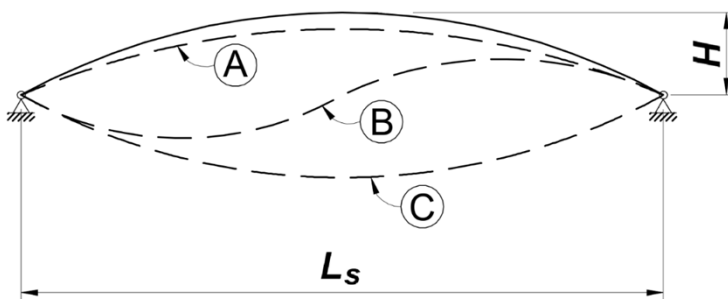


Vertical Truss



In-Plane Strength

Snap-Through Buckling



- A: Deflected shape
- B: Antisymmetric mode
- C: Symmetric mode



In-Plane Strength

Snap-Through Buckling

- Sensitive to second-order effects
- Sensitive to support spreading
- Difficult to predict

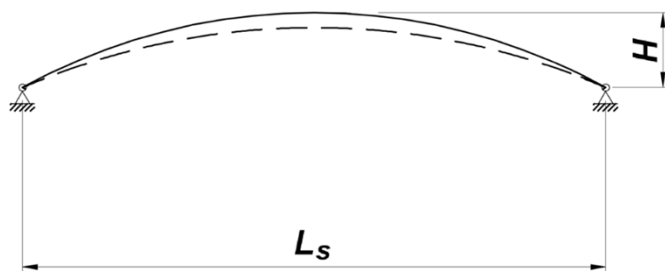


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In-Plane Strength

Snap-Through Buckling

- Generally, not critical for arches with:
 - Rigid supports
 - $H/L_s > 0.2$

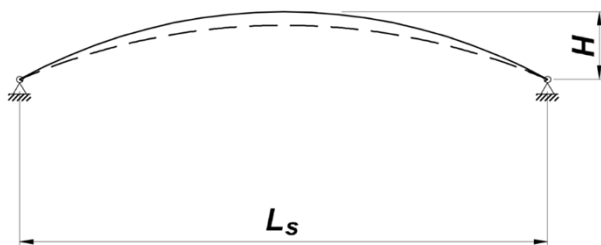


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In-Plane Strength

Snap-Through Buckling

- When $H/L_s \leq 0.2$, L_s/r_i must exceed $(L_s/r_i)_{crit}$



r_i = in-plane radius of gyration



In-Plane Strength

		$(L_s/r_i)_{crit}$		
		H/L_s		
		0.10	0.15	0.20
End Conditions	Pinned	59	36	35
	Fixed	150	71	68



In-Plane Strength

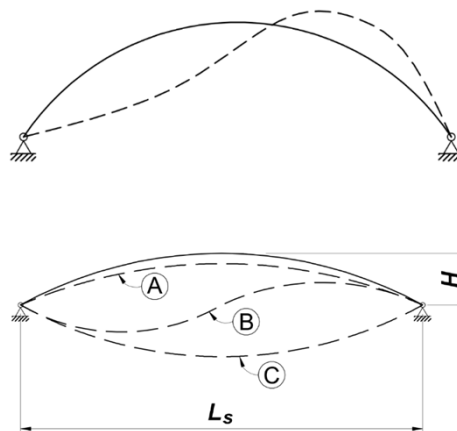
- Design as a straight column
- Flexural buckling provisions in AISC *Specification* Section E3



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In-Plane Strength

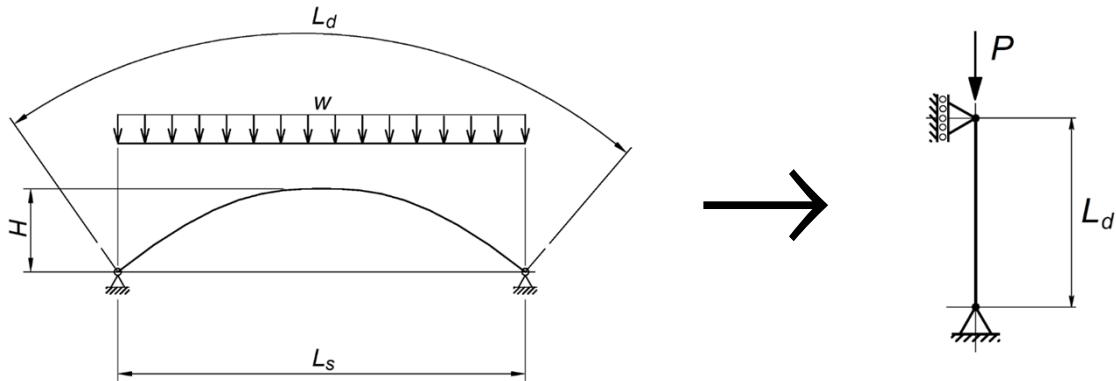
- Applicable only for flexural buckling
- Not valid for snap-through buckling



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In-Plane Strength

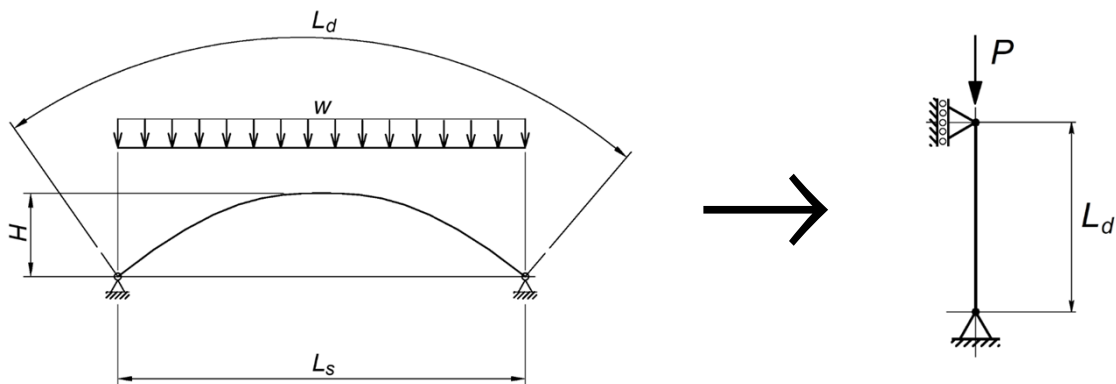
- Unbraced length, $L \rightarrow L_d$



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In-Plane Strength

- $P =$ maximum axial load in the arch



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In-Plane Strength

In-plane effective length factor, K_i			
Arch Form	End Conditions	H/L_s	K_i
Circular	Pinned	$0.1 \leq H/L_s \leq 0.3$	0.55
		$0.3 \leq H/L_s \leq 0.5$	0.60
	Fixed	All	0.40
Parabolic	Pinned	All	0.50
	Fixed	$0.1 \leq H/L_s < 0.3$	0.40
		$0.3 \leq H/L_s \leq 1.0$	0.35



Design of Vertically-Curved Members

Axial Strength

Out-of-Plane Strength

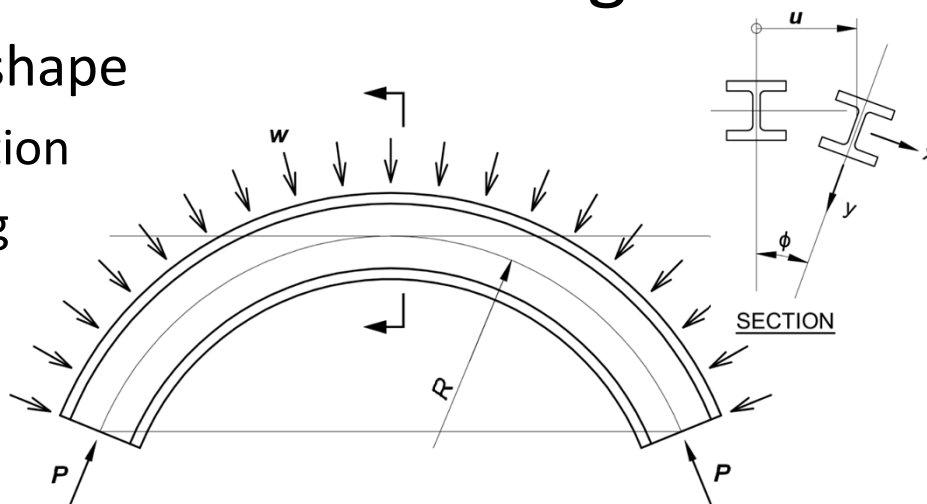


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Out-of-Plane Strength

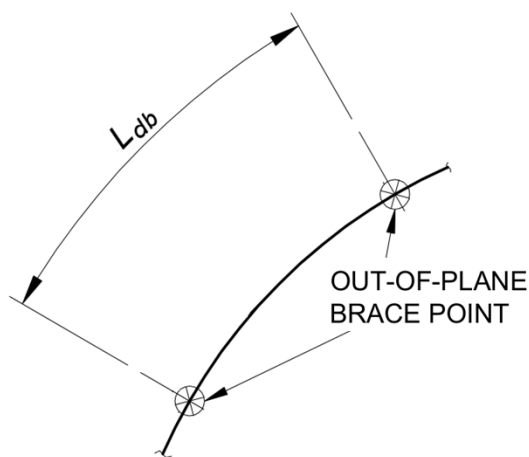
- Buckled shape
 - Translation
 - Twisting



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Out-of-Plane Strength

- Most arches are braced against out-of-plane translation
- Each segment can buckle between brace points



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Out-of-Plane Strength

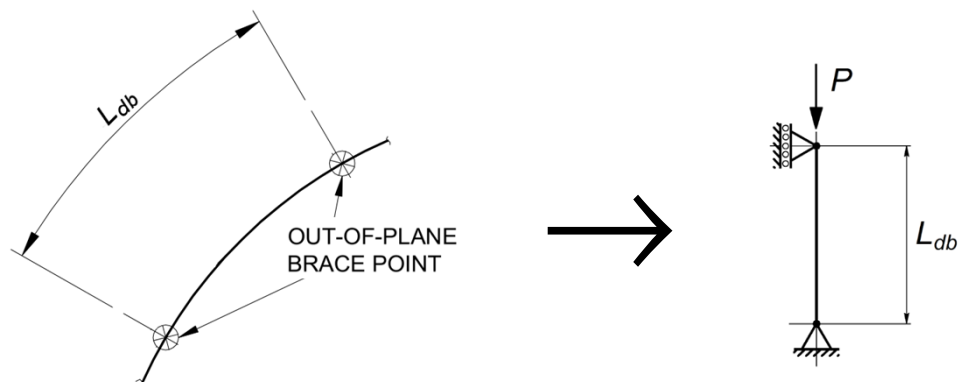
- Design as a straight column
- Flexural buckling provisions in AISC *Specification* Section E3



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Out-of-Plane Strength

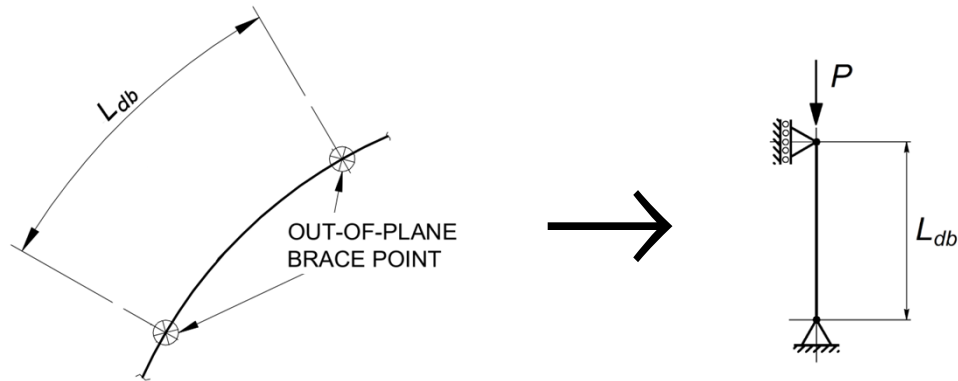
- Unbraced length, $L \rightarrow L_{db}$



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Out-of-Plane Strength

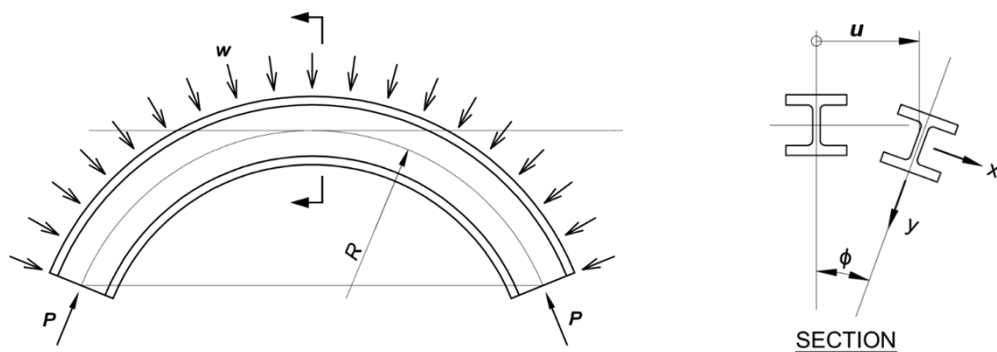
- P = maximum load in the segment



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Out-of-Plane Strength

- Flexural-torsional buckling \rightarrow flexural buckling



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Out-of-Plane Strength

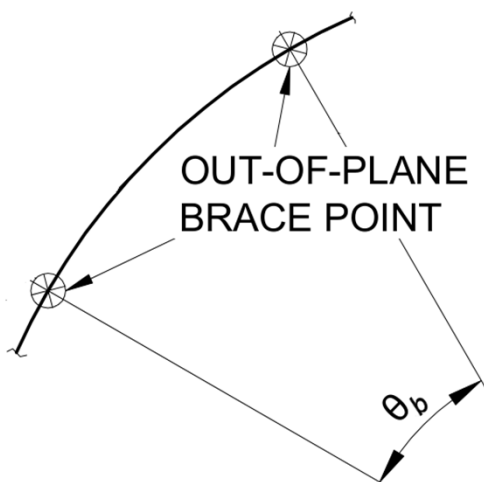
- Effective length factor, K_o : Circular doubly-symmetric segments

$$K_o = \frac{\sqrt{1 + \frac{1}{C_o} \left(\frac{\theta_b}{\pi} \right)^2}}{1 - \left(\frac{\theta_b}{\pi} \right)^2}$$



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Out-of-Plane Strength



θ_b = angle between braces, rad



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Out-of-Plane Strength

$$C_o = \frac{1}{I_o} \left[\frac{GJ}{E} + C_w \left(\frac{\pi}{L_{db}} \right)^2 \right]$$

C_w = warping constant

J = torsional constant

I_o = moment of inertia \perp to the axis of curvature



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Design of Vertically-Curved Members

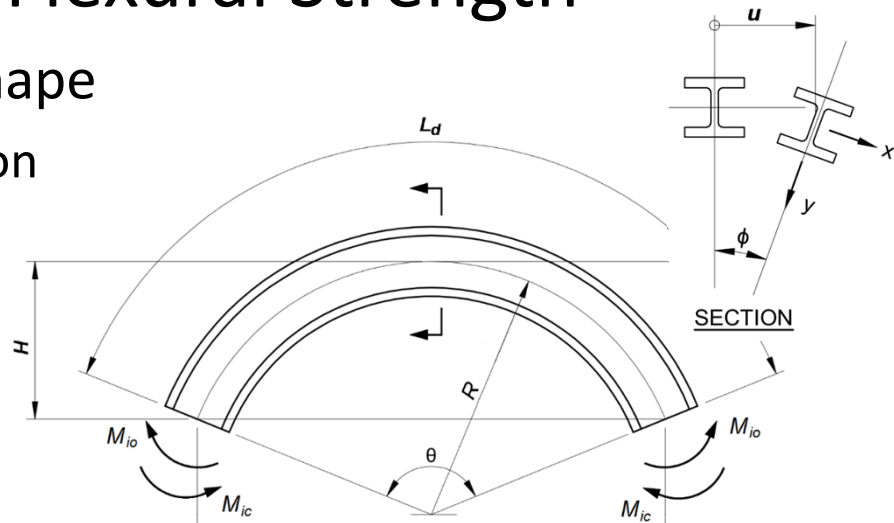
Flexural Strength

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Flexural Strength

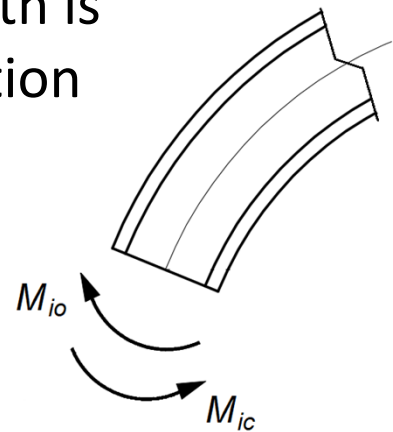
- Buckled shape
 - Translation
 - Twisting



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Flexural Strength

- Lateral-torsional buckling strength is dependent on the loading direction
 - Opening moment, M_{io}
 - Closing moment, M_{ic}



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Flexural Strength

- Design as a straight beam
- Each unbraced segment is treated independently
- AISC *Specification* Chapter F
- Lateral-torsional buckling modification factor, $C_b \rightarrow C_{bi}$

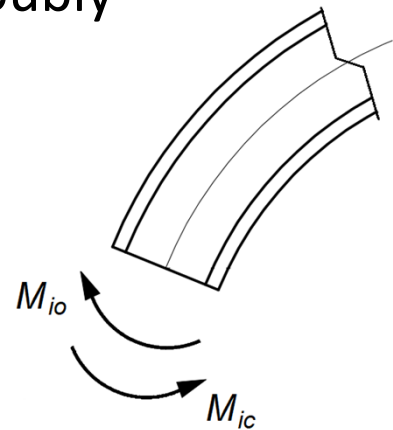


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Flexural Strength

Modification factor, C_{bi} : Circular doubly-symmetric segments

$$C_{bi} = C_{bs} \left(\sqrt{1 + C_a^2 - \frac{C_y C_z}{R^2 M_{es}^2} \pm C_a} \right)$$

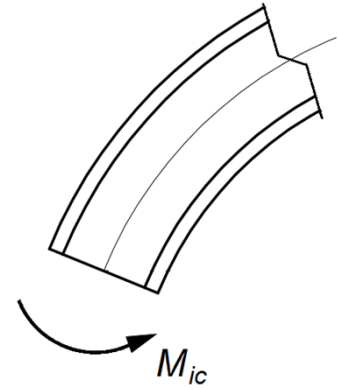


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Flexural Strength

Closing moments → positive root

$$C_{bi} = C_{bs} \left(\sqrt{1 + C_a^2 - \frac{C_y C_z}{R^2 M_{es}^2}} + C_a \right)$$

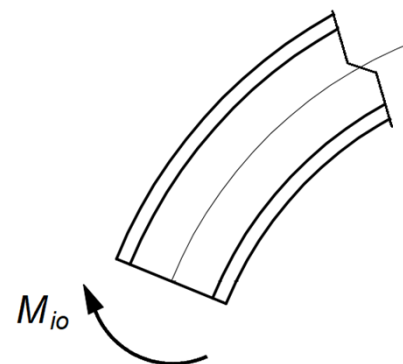


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Flexural Strength

Opening moments → negative root

$$C_{bi} = C_{bs} \left(\sqrt{1 + C_a^2 - \frac{C_y C_z}{R^2 M_{es}^2}} - C_a \right)$$



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Flexural Strength

$C_{bs} = C_b$ for an equivalent straight member (AISC
Specification Equation F1-1)

$$C_b = \frac{12.5M_{max}}{2.5M_{max} + 3M_A + 4M_B + 3M_C}$$

M_{max} = absolute value of max. moment in the segment

$M_{A,B,C}$ = absolute value of moment at $\frac{1}{4}$, $\frac{1}{2}$, $\frac{3}{4}$ points



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Flexural Strength

M_{es} = elastic lateral-torsional buckling moment of
the equivalent straight member subjected to
uniform moment with a length equal to L_{db}

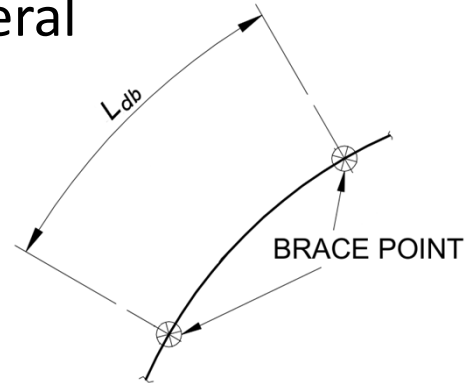
$$M_{es} = \frac{\pi}{L_{db}} \sqrt{EI_o GJ + \left(\frac{\pi E}{L_{db}} \right)^2 I_o C_w}$$



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Flexural Strength

L_{db} = developed length between points that are either braced against lateral displacement of the compression flange or twisting of the cross section



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Flexural Strength

$$C_a = \frac{C_y + C_z}{2RM_{es}}$$

$$C_y = EI_o$$

$$C_z = GJ + \frac{\pi^2 EC_w}{L_{db}^2}$$



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Design of Vertically-Curved Members

Combined Loads



Combined Loads

Axial-Flexure Interaction

- *AISC Specification* Section H1 for doubly-symmetric members



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Combined Loads

Axial-Flexure Interaction

- When $P_r/P_c \geq 0.2$

$$\frac{P_r}{P_c} + \frac{8}{9} \left(\frac{M_r}{M_c} \right) \leq 1.0$$

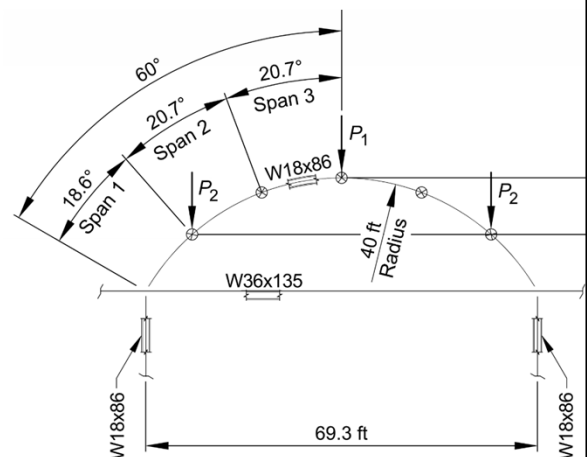
$P_r M_r =$ required strengths $P_c M_c =$ available strengths



Combined Loads

Axial-Flexure Interaction

- Strength must be verified at each segment
- Use the minimum P_r/P_c ratio for each segment



Combined Loads

Axial-Flexure Interaction

- In-plane buckling: P_r/P_c is constant for all segments
- Out-of-plane buckling: both P_r and P_c can vary between segments



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Combined Loads

Second-Order Effects

- Second-order analysis
- Amplified first-order moment: $M_{ri} = B_i M_{i1}$

M_{i1} = first-order moment about the axis of curvature



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Combined Loads

Second-Order Effects

$$B_i = \frac{1}{1 - \alpha \frac{P_r}{P_{ei}}} \quad \begin{array}{l} \alpha = 1.00 \text{ (LRFD)} \\ \quad = 1.60 \text{ (ASD)} \end{array}$$

P_r = maximum axial load in the arch

P_{ei} = elastic critical load for in-plane buckling



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Combined Loads

Second-Order Effects

$$P_{ei} = \frac{\pi^2 E I_i}{(K_i L_d)^2}$$

I_i = moment of inertia about the axis of curvature

K_i = effective length factor for in-plane buckling

L_d = developed length of the arch

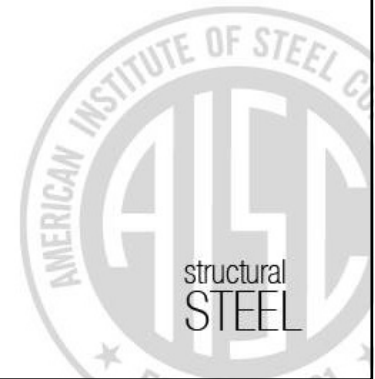


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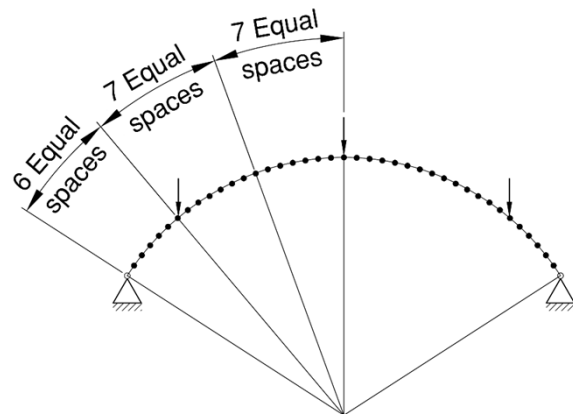
Design of Vertically-Curved Members

Structural Analysis



Structural Analysis

- Curved Members
 - FE Models
 - 2-D beam elements
 - Segmented straight elements



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Structural Analysis

- Accuracy increases with the number of elements
- ≈ 10 to 20 segments for semi-circular members
- For models with highly nonlinear behavior, a convergence study may be required



91

Structural Analysis

- Where deflections are significant, a 2nd-order FE analysis is required
- 2nd-order effects are not captured with a traditional P - Δ FE analysis because arch deformations cause vertical, not horizontal, translation of the gravity loads



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Structural Analysis

- A 2nd-order FE analysis must properly consider in-plane deformations
 - member axial shortening
 - horizontal support flexibility



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Design of Vertically-Curved Members

Local Strength

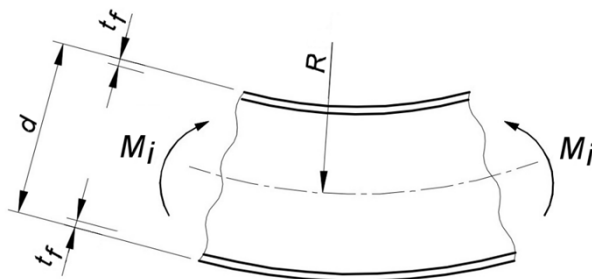
There's always a solution in steel.



Local Strength

Cross-Sectional Distortion

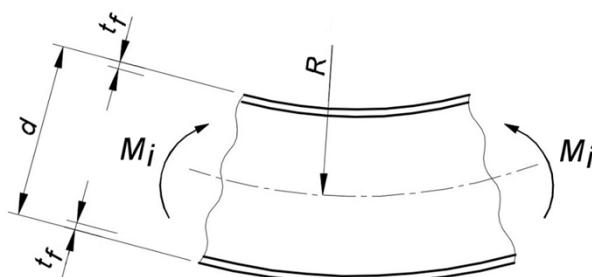
- Flexure in the plane of curvature



Local Strength

Cross-Sectional Distortion

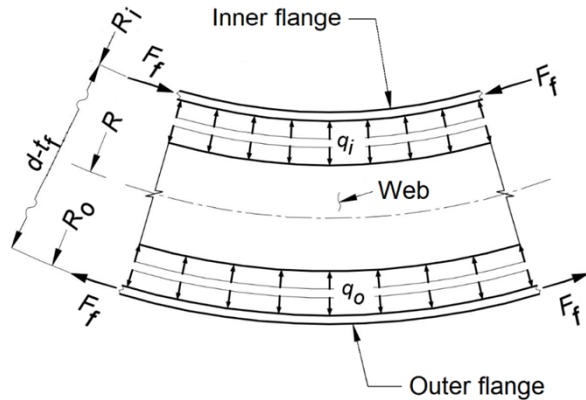
- Can reduce flexural strength and stiffness



Local Strength

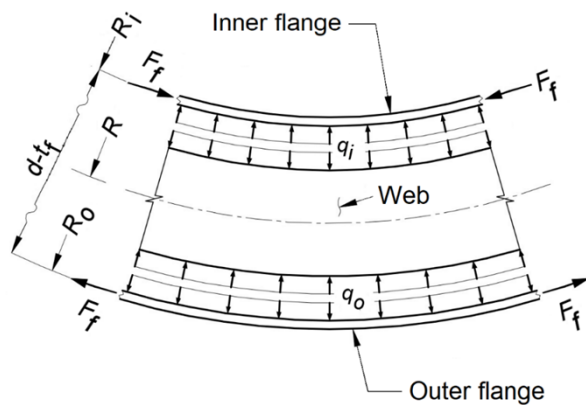
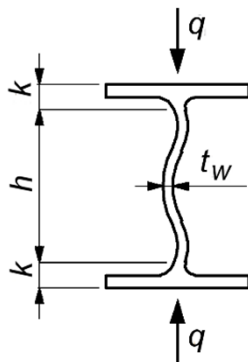
Cross-Sectional Distortion

- Radial forces at web-to-flange interfaces



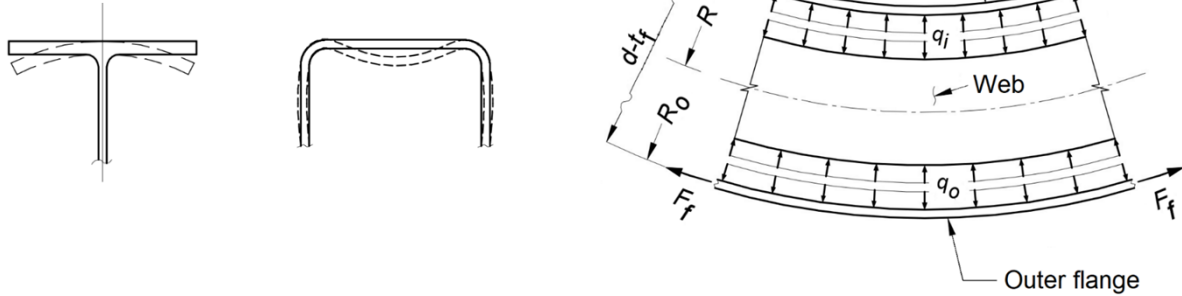
Local Strength

Web Bend-Buckling



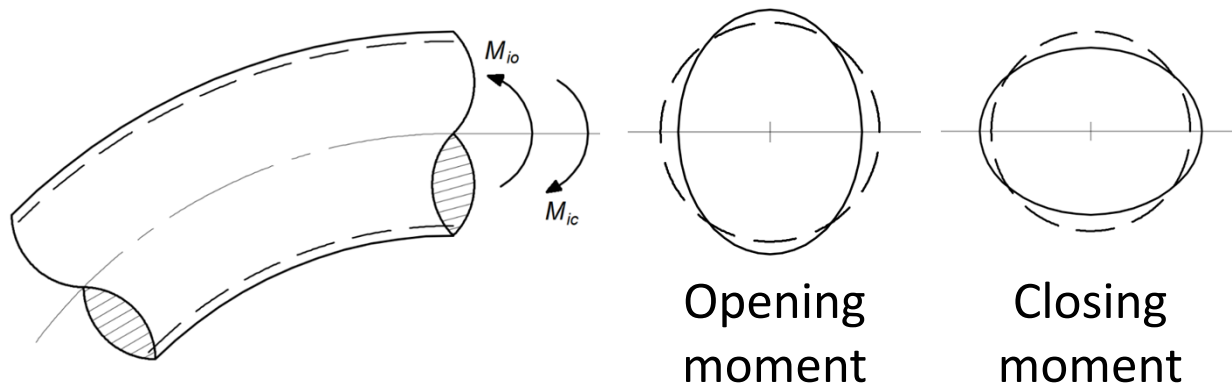
Local Strength

Element Local Bending



Local Strength

Ovalization



Local Strength

Element Local Bending

Two design methods are available:

1. General method

- Explicit calculation of the element local bending strength
- Applicable to all flat elements



101

Local Strength

Element Local Bending

2. Simplified method

- Reduced flexural properties account for local bending
- Applicable only to I-Shape and HSS Members



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There's always a solution in steel.

Design of Vertically-Curved Members

Local Strength

Simplified Method



Simplified Method

Effective Flexural Properties (Flat Elements)

- Effective section modulus: $S_{ei} = k_f S_i$
- Effective plastic modulus: $Z_{ei} = k_f Z_i$
- Effective moment of inertia: $I_{ei} = k_f I_i$

I_i, S_i, Z_i = flexural properties of a straight member about the axis of curvature



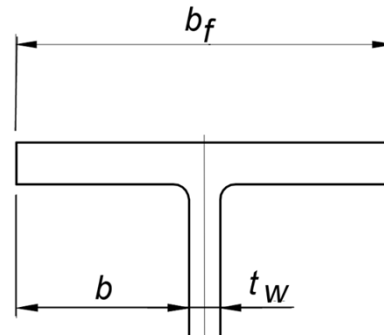
104

Simplified Method

Effective Flexural Properties

- I-shape members

$$k_f = \frac{9.20}{8.80 + \frac{b_f^2}{Rt_f}} \leq 1.00$$



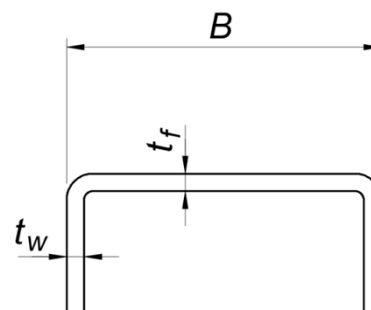
105

Simplified Method

Effective Flexural Properties

- Rectangular HSS members

$$k_f = \frac{8.24}{7.44 + \frac{(B - t_w)^2}{Rt_f}} \leq 1.00$$



106

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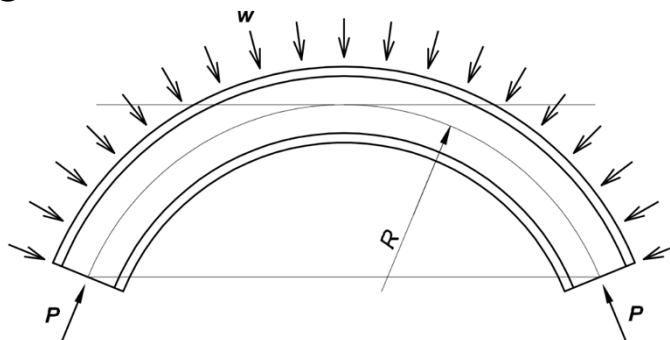
Design of Vertically-Curved Members

Connections



Connections

- Arch behavior produces large horizontal reactions

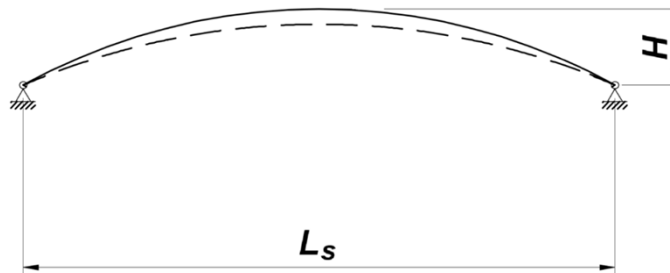


108



Connections

- Arch stability is dependent on horizontal connection rigidity



109

Connections

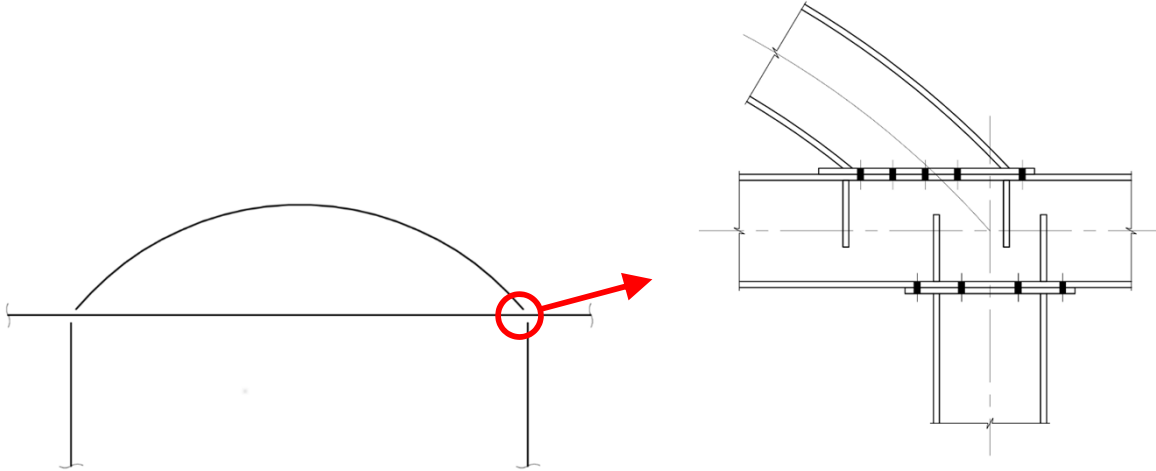
End Plate Connections

- Efficient for compression load transfer
- Member ends must be cut accurately to eliminate gaps

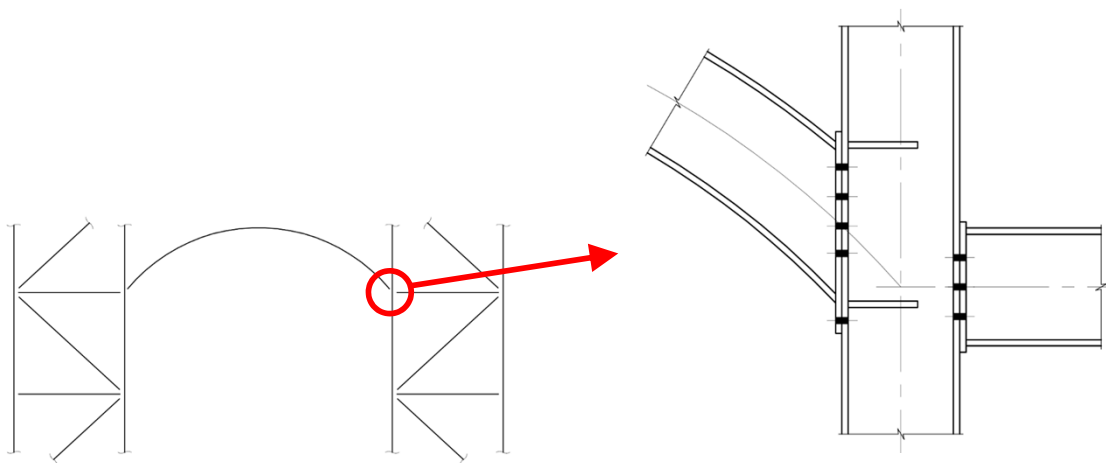


110

Connections



Connections



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Question time



Individual Webinar Registrants

CEU/PDH Certificates

Within 2 business days...

- You will receive an email on how to report attendance from: registration@aisc.org.
- Be on the lookout: Check your spam filter! Check your junk folder!
- Completely fill out online form. Don't forget to check the boxes next to each attendee's name!



Individual Webinar Registrants

CEU/PDH Certificates

Within 2 business days...

- New reporting site (URL will be provided in the forthcoming email).
- Username: Same as AISC website username.
- Password: Same as AISC website password.



8-Session Registrants

CEU/PDH Certificates

One certificate will be issued at the conclusion of
all 8 sessions.



8-Session Registrants

Access to the quiz: Information for accessing the quiz will be emailed to you by Wednesday. It will contain a link to access the quiz. EMAIL COMES FROM NIGHTSCHOOL@AISC.ORG

Quiz and Attendance records: Posted Tuesday mornings.
www.aisc.org/nightschool - click on Current Course Details.

Reasons for quiz:

- EEU – must take all quizzes and final to receive EEU
- CEUs/PDHS – If you watch a recorded session you must take quiz for CEUs/PDHS.
- REINFORCEMENT – Reinforce what you learned tonight. Get more out of the course.

NOTE: If you attend the live presentation, you do not have to take the quizzes to receive CEUs/PDHS.



8-Session Registrants

Access to the recording: Information for accessing the recording will be emailed to you by this Wednesday. The recording will be available for three weeks. For 8-session registrants only. EMAIL COMES FROM NIGHTSCHOOL@AISC.ORG.

CEUs/PDHS – If you watch a recorded session you must take AND PASS the quiz for CEUs/PDHS.



Night School Resources for 8-session package Registrants

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Night School 13: Design of Industrial Buildings

8-SESSION PACKAGE RESOURCES

Event	Date	Handouts	Video	Quiz	Attendance
NS13 - Design Criteria	1/30/2017 7:00:00 PM	Handouts	View Passcode: NS13DSN	Pass Score: 80	Pending
NS13 - Economic Considerations	2/6/2017 7:00:00 PM	Handouts	Available 02/08/2017 5pm EST	Available 02/08/2017 5pm EST	Pending
NS13 - Lateral Load Systems and Details	2/13/2017 7:00:00 PM	Handouts	Available 02/15/2017 5pm EST	Available 02/15/2017 5pm EST	Pending
NS13 - Preliminary Design Procedures	2/27/2017 7:00:00 PM	Handouts	Available 03/01/2017 5pm EST	Available 03/01/2017 5pm EST	Pending
NS13 - Crane Girder Design and Frame Analysis	3/6/2017 7:00:00 PM	Handouts	Available 03/08/2017 5pm EST	Available 03/08/2017 5pm EST	Pending
NS13 - Frame Member and Connection Design	3/13/2017 7:00:00 PM	Handouts	Available 03/15/2017 5pm EST	Available 03/15/2017 5pm EST	Pending
NS13 - Transfer Crane Girder & Longitudinal Bldg Bracing Dsn	3/27/2017 7:00:00 PM	Handouts	Available 03/29/2017 5pm EST	Available 03/29/2017 5pm EST	Pending
NS13 - Building Envelope and Bracing Design	4/3/2017 7:00:00 PM	Handouts	Available 04/05/2017 5pm EST	Available 04/05/2017 5pm EST	Pending
NS13 - Final Exam	4/10/2017 7:00:00 PM			Available 04/12/2017 5pm EST	



Night School Resources for 8-session package Registrants

- Weekly “quiz and recording” email.
- Weekly updates of the master Quiz and Attendance record found at www.aisc.org/nightschool. Scroll down to Quiz and Attendance records.
 - Updated on Tuesday mornings.



Night School Resources for 8-session package Registrants

- Webinar connection information:
 - Found in your registration confirmation/receipt.
 - Reminder email sent out Monday mornings.
- Link to handouts also found here.



There's always a solution in steel.

Thank You

Please give us your feedback!
Survey at conclusion of webinar.

