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 Session Description


Session 2: Design of Vertically Curved Members
June 25, 2018

This session first addresses general design considerations including architecturally exposed structural steel, tolerances and contract documents. The presentation then addresses the treatment vertically-curved members. Topics include axial strength, flexural strength, combined axial and flexural loads, local strength and connections.

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 Learning Objectives

- Identify the 5 categories of Architecturally Exposed Structural Steel (AESS) stated in the 2016 AISC Code of Standard Practice.
- Identify the tolerances for curved steel members stated in the 2016 AISC Code of Standard Practice.
- Describe the design considerations for axial strength of vertically-curved members in terms of in-plane and out-of-plane strength.
- Describe the design considerations for flexural strength of vertically-curved members.

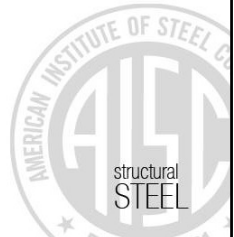
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Design of Curved Members
Session 2: Design of Vertically Curved Members
June 25, 2018

Presented by
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ARC International, LLC
Birmingham, AL




There's always a solution in steel.



There's always a solution in steel.


General Information on Curved Members

Session Description



Session Description

- General Design Considerations
 - Architecturally exposed members
 - Tolerances
 - Contract documents




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Design of Vertically-Curved Members

Session Description



Session Description

- Vertically-curved members
 - Axial strength
 - Flexural strength
 - Combined loads(continued)



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Session Description

- Structural analysis
- Local strength
- Connections



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General Information on Curved Members

General Design Considerations

Architecturally Exposed (AESS)
Members

There's always a solution in steel.



AESS Members

2016 AISC Code of Standard Practice (COSP)

- AISC Code of Standard Practice Section 10.1.1 defines five categories of AESS:
 - AESS 1: Basic elements
 - AESS 2: Feature elements viewed at > 20 ft
- (continued)



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AESS Members

- AESS 3: Feature elements viewed at < 20 ft
- AESS 4: Showcase elements
- AESS C: Custom elements

The 2016 COSP is available for free download at:

<https://www.aisc.org/globalassets/aisc/publications/standards/code-of-standard-practice-june-15-2016.pdf>



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AESS Members

- For further information on AESS, see the Nov. 2017 issue of *Modern Steel Construction*:
https://www.aisc.org/globalassets/aisc/aess/aess_11_about_aess_reprint.pdf
- Generally, the bending cost increases with increasing AESS category



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AESS Members

- Generally, the bending cost increases with increasing AESS category



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General Information on Curved Members

General Design Considerations

Tolerances

There's always a solution in steel.



Tolerances

2016 AISC Code of Standard Practice (COSP)

- Chord length tolerance
- Curvature tolerance
- Similar to those for straight members
- Tolerances for AESS are the same as non-AESS



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Tolerances

2016 AISC Code of Standard Practice (COSP)

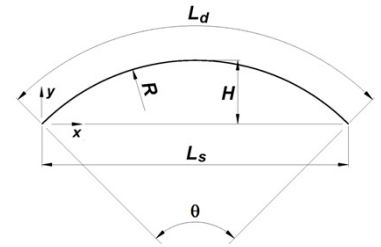
- No cross-sectional distortion tolerance
- Tolerances that are not addressed in the COSP should be mutually agreed upon by the contractor and the owner



Tolerances

Chord Length Tolerance

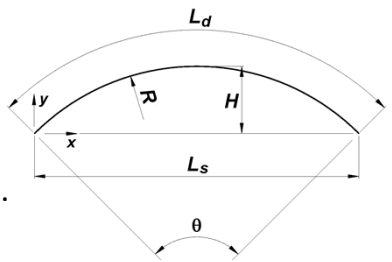
- Tolerance on L_s
- COSP Section 6.4.2(b)



Tolerances

Chord Length Tolerance

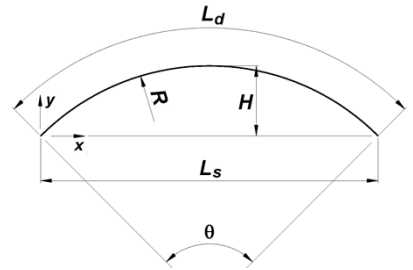
- Members that frame to other structural steel elements:
 - For $L_s \leq 30$ ft: $\pm 1/16$ in.
 - For $L_s > 30$ ft: $\pm 1/8$ in.



Tolerances

Curvature Tolerance

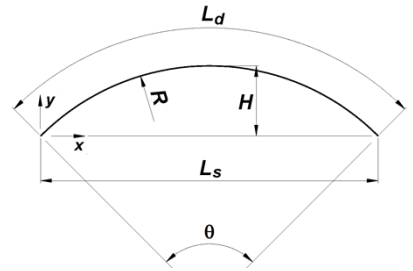
- Tolerance on H
- Non-AESS: COSP Section 6.4.2(b)
- AESS: COSP Section 10.4.4



Tolerances

Curvature Tolerance

- Dependent on L_d



Tolerances

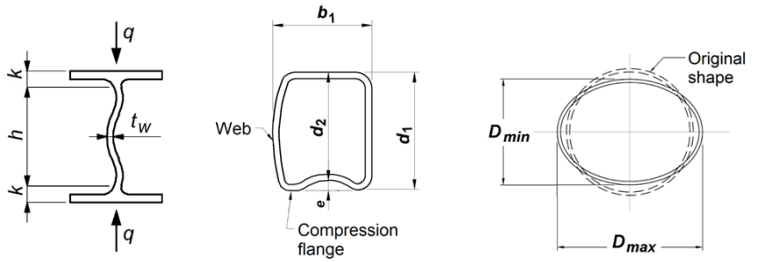
Curvature Tolerance

- Equal to the camber and sweep tolerances for straight members in the applicable ASTM standard
- Sharp kinks or sharp bends are cause for rejection



Tolerances

Distortion Tolerance



Tolerances

Distortion Tolerance

- Should be based on:
 - The potential effect on structural performance
 - Any aesthetic requirements for AESS members
- Should be established with input from the bender/roller



Tolerances

Distortion Tolerance: Structural Effects

- Reasonable cross-sectional distortions can be tolerated without a reduction in strength
- See Design Guide Section 5.5 for further information



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Tolerances

Distortion Tolerance: AESS

- Generally, AESS requirements are more stringent than strength requirements
- Members with large- and medium-radius bends are likely to be acceptable for AESS 1 and 2 without further consideration



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Tolerances

Distortion Tolerance

- Cross-sectional tolerances specified in ASTM A6, ASTM A53 and ASTM A500 are mill tolerances
- Initial geometric imperfections are amplified during the bending process



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Tolerances

Distortion Tolerance: Rectangular HSS

- The permissible cross-sectional variation for ASTM A500 rectangular HSS members larger than 5½ in. is 1% of the largest outside flat dimension

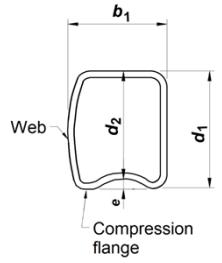


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Tolerances

Distortion Tolerance: Rectangular HSS

- Post-bending wall flatness tolerances (ρ_w and ρ_f) between 1% and 2% are common

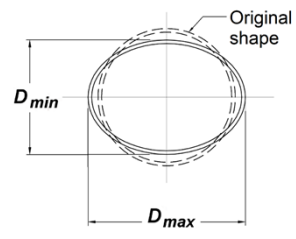


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Tolerances

Distortion Tolerance: Round HSS

- A post-bending ovality tolerance (ρ) of 5% is common



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Tolerances

Distortion Tolerance: Round HSS

- Practical considerations may dictate more stringent tolerances

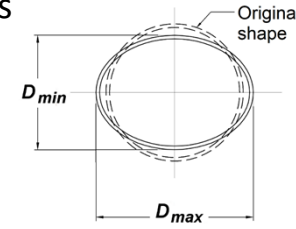


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Tolerances

Distortion Tolerance: Round HSS

- Example: when two segments are connected with circumferential butt welds, proper wall alignment is essential




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Tolerances

Distortion Tolerance: Round HSS

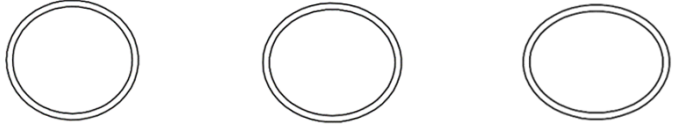
- For AESS, a 5% tolerance is likely to produce imperceptible ovalization distortions




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Tolerances

Distortion Tolerance: Round HSS



$\rho = 5\%$ $\rho = 8\%$ $\rho = 12\%$




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General Information on Curved Members

General Design Considerations


Contract Documents



Contract Documents

Member Sizes

- Often controlled by bending requirements rather than performance under service loads
- Member sizes shown on the design drawings should consider bending requirements



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Contract Documents

Architecturally Exposed (AESS) Members

- All AESS members must be identified in the contract documents
- AESS members must be assigned a category defined in AISC *Code of Standard Practice* Section 10.1.1



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Contract Documents

Distortion Tolerances

- Distortion tolerances should be specified in the contract documents



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Design of Vertically-Curved Members

Axial Strength

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Axial Strength

Arches

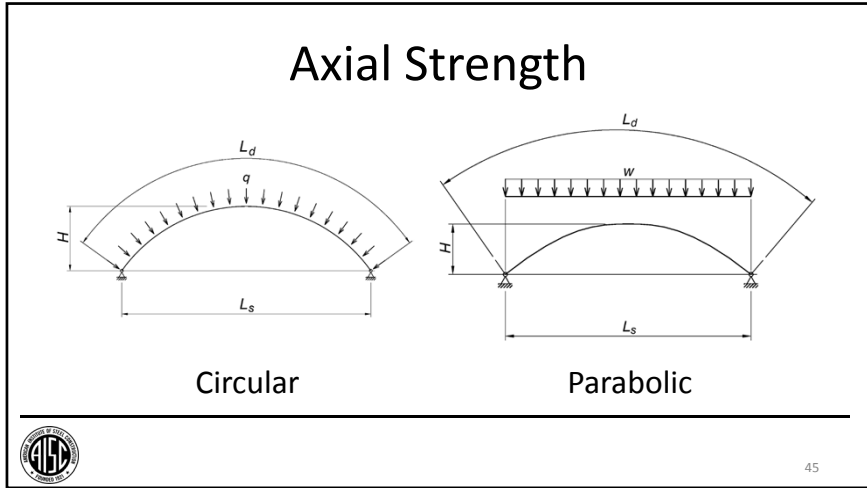
- Structurally efficient
- Loads carried primarily by compression



Photograph courtesy of the AISC Bender/Roller Committee



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Design of Vertically-Curved Members

Axial Strength

In-Plane Strength

In-Plane Strength

- Curved Members \neq Straight Members
- Buckled Shape

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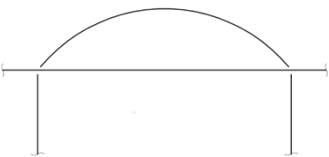
In-Plane Strength

- Support spreading
 - Increases deflection
 - Can lead to collapse

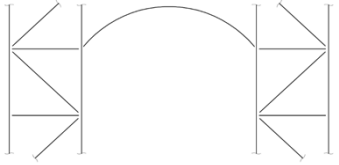
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In-Plane Strength


- Horizontal restraints



Tension Tie

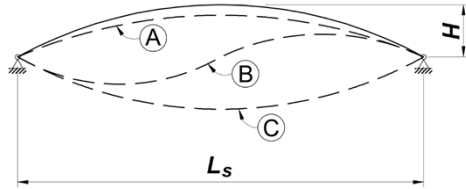


Vertical Truss



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In-Plane Strength

Snap-Through Buckling




A: Deflected shape
 B: Antisymmetric mode
 C: Symmetric mode


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In-Plane Strength

Snap-Through Buckling

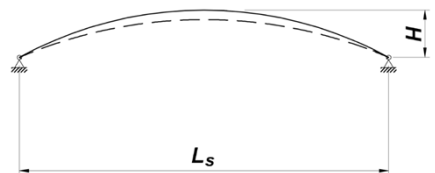
- Sensitive to second-order effects
- Sensitive to support spreading
- Difficult to predict



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In-Plane Strength

Snap-Through Buckling

- Generally, not critical for arches with:
 - Rigid supports
 - $H/L_s > 0.2$

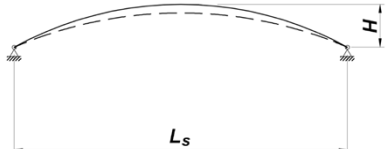



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In-Plane Strength

Snap-Through Buckling

- When $H/L_s \leq 0.2$, L_s/r_i must exceed $(L_s/r_i)_{crit}$




r_i = in-plane radius of gyration


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In-Plane Strength

		$(L_s/r_i)_{crit}$		
		H/L_s		
		0.10	0.15	0.20
End Conditions	Pinned	59	36	35
	Fixed	150	71	68


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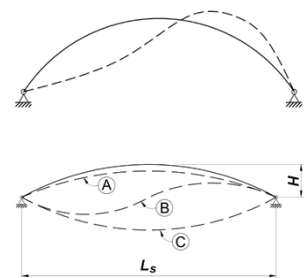
In-Plane Strength


- Design as a straight column
- Flexural buckling provisions in AISC *Specification* Section E3


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In-Plane Strength


- Applicable only for flexural buckling
- Not valid for snap-through buckling




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In-Plane Strength

- Unbraced length, $L \rightarrow L_d$


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In-Plane Strength

- $P =$ maximum axial load in the arch


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In-Plane Strength

In-plane effective length factor, K_i			
Arch Form	End Conditions	H/L_s	K_i
Circular	Pinned	$0.1 \leq H/L_s \leq 0.3$	0.55
		$0.3 \leq H/L_s \leq 0.5$	0.60
	Fixed	All	0.40
Parabolic	Pinned	All	0.50
	Fixed	$0.1 \leq H/L_s < 0.3$	0.40
		$0.3 \leq H/L_s \leq 1.0$	0.35




Design of Vertically-Curved Members

Axial Strength

Out-of-Plane Strength

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Out-of-Plane Strength

- Buckled shape
 - Translation
 - Twisting

The diagram shows a semi-circular arch with a radius R and a central angle of 90° . It is subjected to a uniformly distributed load w acting downwards. At the base of the arch, there are reaction forces P . The buckled shape is shown as a dashed line, indicating out-of-plane translation u and twisting ϕ . A cross-section labeled 'SECTION' shows the I-beam profile with its x and y axes.

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Out-of-Plane Strength

- Most arches are braced against out-of-plane translation
- Each segment can buckle between brace points

The diagram shows a curved member segment between two 'OUT-OF-PLANE BRACE POINTS'. The unbraced length between these points is labeled L_{db} .

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Out-of-Plane Strength

- Design as a straight column
- Flexural buckling provisions in AISC *Specification* Section E3

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Out-of-Plane Strength

- Unbraced length, $L \rightarrow L_{db}$

The diagram illustrates the conversion of the unbraced length L of a curved member to the design unbraced length L_{db} . It shows a curved member with two brace points and an arrow pointing to a straight column of length L_{db} under a load P .

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Out-of-Plane Strength

- P = maximum load in the segment

OUT-OF-PLANE BRACE POINT

L_{db}

L_{db}

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Out-of-Plane Strength

- Flexural-torsional buckling → flexural buckling

SECTION

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Out-of-Plane Strength

- Effective length factor, K_o : Circular doubly-symmetric segments

$$K_o = \frac{\sqrt{1 + \frac{1}{C_o} \left(\frac{\theta_b}{\pi}\right)^2}}{1 - \left(\frac{\theta_b}{\pi}\right)^2}$$

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Out-of-Plane Strength

OUT-OF-PLANE BRACE POINT

θ_b = angle between braces, rad

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Out-of-Plane Strength

$$C_o = \frac{1}{I_o} \left[\frac{GJ}{E} + C_w \left(\frac{\pi}{L_{db}} \right)^2 \right]$$

C_w = warping constant
 J = torsional constant
 I_o = moment of inertia \perp to the axis of curvature



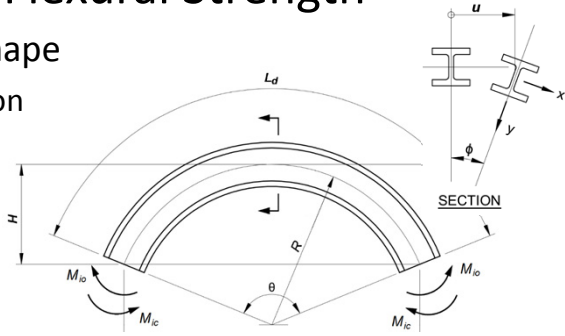
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Design of Vertically-Curved Members

Flexural Strength

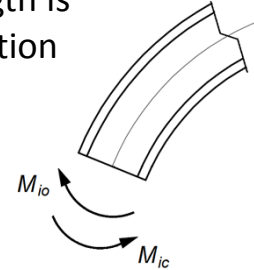
Flexural Strength

- Buckled shape
 - Translation
 - Twisting




Flexural Strength

- Lateral-torsional buckling strength is dependent on the loading direction
 - Opening moment, M_{io}
 - Closing moment, M_{ic}



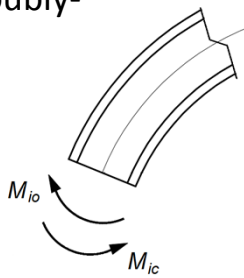
Flexural Strength


- Design as a straight beam
- Each unbraced segment is treated independently
- AISC *Specification* Chapter F
- Lateral-torsional buckling modification factor, $C_b \rightarrow C_{bi}$


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Flexural Strength

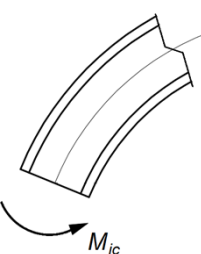
Modification factor, C_{bi} : Circular doubly-symmetric segments


$$C_{bi} = C_{bs} \left(\sqrt{1 + C_a^2 - \frac{C_y C_z}{R^2 M_{es}^2} \pm C_a} \right)$$



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Flexural Strength

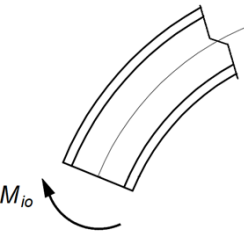
Closing moments \rightarrow positive root


$$C_{bi} = C_{bs} \left(\sqrt{1 + C_a^2 - \frac{C_y C_z}{R^2 M_{es}^2} + C_a} \right)$$



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Flexural Strength

Opening moments \rightarrow negative root

$$C_{bi} = C_{bs} \left(\sqrt{1 + C_a^2 - \frac{C_y C_z}{R^2 M_{es}^2} - C_a} \right)$$



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Flexural Strength

$C_{bs} = C_b$ for an equivalent straight member (AISC Specification Equation F1-1)

$$C_b = \frac{12.5M_{max}}{2.5M_{max} + 3M_A + 4M_B + 3M_C}$$

M_{max} = absolute value of max. moment in the segment

$M_{A,B,C}$ = absolute value of moment at $\frac{1}{4}$, $\frac{1}{2}$, $\frac{3}{4}$ points



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Flexural Strength

M_{es} = elastic lateral-torsional buckling moment of the equivalent straight member subjected to uniform moment with a length equal to L_{db}

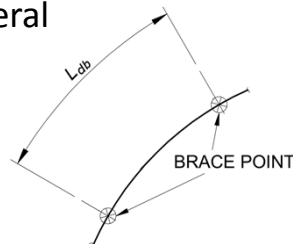
$$M_{es} = \frac{\pi}{L_{db}} \sqrt{EI_o GJ + \left(\frac{\pi E}{L_{db}}\right)^2 I_o C_w}$$



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Flexural Strength

L_{db} = developed length between points that are either braced against lateral displacement of the compression flange or twisting of the cross section



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Flexural Strength

$$C_a = \frac{C_y + C_z}{2RM_{es}}$$

$$C_y = EI_o$$


$$C_z = GJ + \frac{\pi^2 EC_w}{L_{db}^2}$$



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Design of Vertically-Curved Members


Combined Loads



Combined Loads

Axial-Flexure Interaction

- AISC *Specification* Section H1 for doubly-symmetric members



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Combined Loads

Axial-Flexure Interaction

- When $P_r/P_c \geq 0.2$

$$\frac{P_r}{P_c} + \frac{8}{9} \left(\frac{M_r}{M_c} \right) \leq 1.0$$

P_r, M_r = required strengths P_c, M_c = available strengths

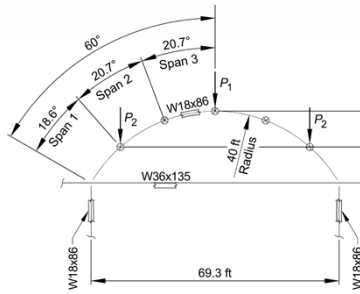



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Combined Loads

Axial-Flexure Interaction

- Strength must be verified at each segment
- Use the minimum P_r/P_c ratio for each segment

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Combined Loads

Axial-Flexure Interaction

- In-plane buckling: P_r/P_c is constant for all segments
- Out-of-plane buckling: both P_r and P_c can vary between segments



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Combined Loads

Second-Order Effects

- Second-order analysis
- Amplified first-order moment: $M_{ri} = B_i M_{i1}$

M_{i1} = first-order moment about the axis of curvature



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Combined Loads

Second-Order Effects

$$B_i = \frac{1}{1 - \alpha \frac{P_r}{P_{ei}}} \quad \begin{array}{l} \alpha = 1.00 \text{ (LRFD)} \\ \alpha = 1.60 \text{ (ASD)} \end{array}$$

P_r = maximum axial load in the arch

P_{ei} = elastic critical load for in-plane buckling



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Combined Loads

Second-Order Effects

$$P_{ei} = \frac{\pi^2 E I_i}{(K_i L_d)^2}$$

I_i = moment of inertia about the axis of curvature

K_i = effective length factor for in-plane buckling

L_d = developed length of the arch




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Design of Vertically-Curved Members


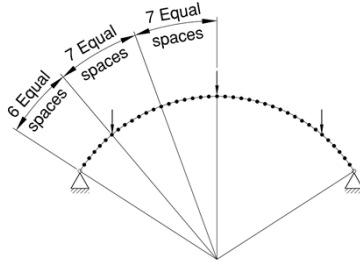
Structural Analysis



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Structural Analysis


- Curved Members
 - FE Models
 - 2-D beam elements
 - Segmented straight elements



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Structural Analysis


- Accuracy increases with the number of elements
- ≈ 10 to 20 segments for semi-circular members
- For models with highly nonlinear behavior, a convergence study may be required



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Structural Analysis

- Where deflections are significant, a 2nd-order FE analysis is required
- 2nd-order effects are not captured with a traditional $P-\Delta$ FE analysis because arch deformations cause vertical, not horizontal, translation of the gravity loads



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Structural Analysis

- A 2nd-order FE analysis must properly consider in-plane deformations
 - member axial shortening
 - horizontal support flexibility



Design of Vertically-Curved Members

Local Strength

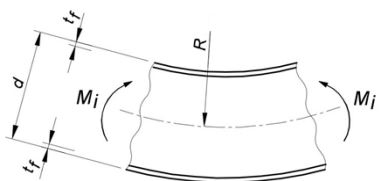
There's always a solution in steel.



Local Strength

Cross-Sectional Distortion

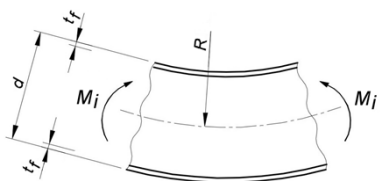
- Flexure in the plane of curvature



Local Strength

Cross-Sectional Distortion

- Can reduce flexural strength and stiffness



Local Strength

Cross-Sectional Distortion

- Radial forces at web-to-flange interfaces

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Local Strength

Web Bend-Buckling

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Local Strength

Element Local Bending

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Local Strength

Ovalization

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Local Strength

Element Local Bending

Two design methods are available:

1. General method
 - Explicit calculation of the element local bending strength
 - Applicable to all flat elements



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Local Strength

Element Local Bending

2. Simplified method
 - Reduced flexural properties account for local bending
 - Applicable only to I-Shape and HSS Members



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Design of Vertically-Curved Members

Local Strength

Simplified Method



There's always a solution in steel.

Simplified Method

Effective Flexural Properties (Flat Elements)

- Effective section modulus: $S_{ei} = k_f S_i$
- Effective plastic modulus: $Z_{ei} = k_f Z_i$
- Effective moment of inertia: $I_{ei} = k_f I_i$

I_i, S_i, Z_i = flexural properties of a straight member about the axis of curvature

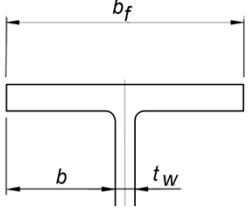



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Simplified Method

Effective Flexural Properties

- I-shape members

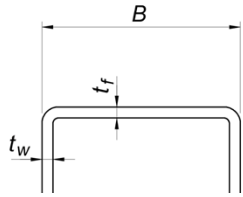
$$k_f = \frac{9.20}{8.80 + \frac{b_f^2}{Rt_f}} \leq 1.00$$




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Simplified Method

Effective Flexural Properties

- Rectangular HSS members


$$k_f = \frac{8.24}{7.44 + \frac{(B-t_w)^2}{Rt_f}} \leq 1.00$$




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Design of Vertically-Curved Members

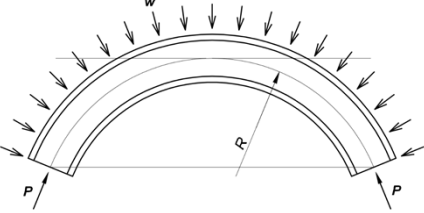
Connections





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Connections

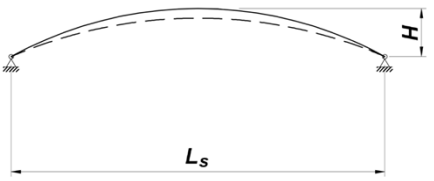
- Arch behavior produces large horizontal reactions




108

Connections

- Arch stability is dependent on horizontal connection rigidity



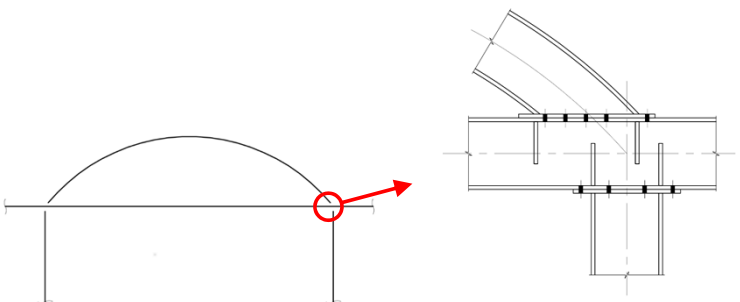
Connections

End Plate Connections

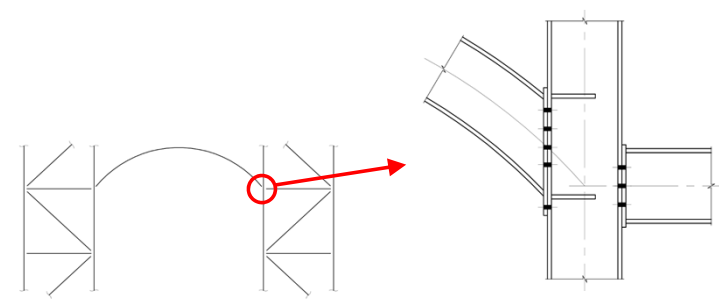
- Efficient for compression load transfer
- Member ends must be cut accurately to eliminate gaps



Connections




Connections



There's always a solution in steel.

Question time




Individual Webinar Registrants

CEU/PDH Certificates

Within 2 business days...

- You will receive an email on how to report attendance from: registration@aisc.org.
- Be on the lookout: Check your spam filter! Check your junk folder!
- Completely fill out online form. Don't forget to check the boxes next to each attendee's name!




Individual Webinar Registrants

CEU/PDH Certificates

Within 2 business days...

- New reporting site (URL will be provided in the forthcoming email).
- Username: Same as AISC website username.
- Password: Same as AISC website password.



8-Session Registrants

CEU/PDH Certificates

One certificate will be issued at the conclusion of all 8 sessions.



8-Session Registrants

Access to the quiz: Information for accessing the quiz will be emailed to you by Wednesday. It will contain a link to access the quiz. EMAIL COMES FROM NIGHTSCHOOL@AISC.ORG

Quiz and Attendance records: Posted Tuesday mornings.
www.aisc.org/nightschool - click on Current Course Details.

Reasons for quiz:

- EEU – must take all quizzes and final to receive EEU
- CEUs/PDHS – If you watch a recorded session you must take quiz for CEUs/PDHS.
- REINFORCEMENT – Reinforce what you learned tonight. Get more out of the course.

NOTE: If you attend the live presentation, you do not have to take the quizzes to receive CEUs/PDHS.



8-Session Registrants

Access to the recording: Information for accessing the recording will be emailed to you by this Wednesday. The recording will be available for three weeks. For 8-session registrants only. EMAIL COMES FROM NIGHTSCHOOL@AISC.ORG.

CEUs/PDHS – If you watch a recorded session you must take AND PASS the quiz for CEUs/PDHS.



Night School Resources for 8-session package Registrants

Find all your handouts, quizzes and quiz scores, recording access, and attendance information all in one place!



Night School Resources for 8-session package Registrants

Go to www.aisc.org and sign in.



Login

If you're an existing customer, please enter your username and password.

USERNAME
Enter your username

PASSWORD
Enter your password

Remember Me

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[REGISTER NOW](#)

Night School Resources for 8-session package Registrants

Go to www.aisc.org and sign in.

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Night School Resources for 8-session package Registrants

Night School 13: Design of Industrial Buildings

8-SESSION PACKAGE RESOURCES

Event	Date	Handouts	Video	Quiz	Attendance
NS13 - Design Criteria	1/30/2017 7:00:00 PM	Handouts	Video	Pass Score: 80	Pending
NS13 - Economic Considerations	2/6/2017 7:00:00 PM	Handouts	Available 02/06/2017 5pm EST	Available 02/08/2017 5pm EST	Pending
NS13 - Lateral Load Systems and Details	2/13/2017 7:00:00 PM	Handouts	Available 02/13/2017 5pm EST	Available 02/15/2017 5pm EST	Pending
NS13 - Preliminary Design Procedures	2/27/2017 7:00:00 PM	Handouts	Available 03/01/2017 5pm EST	Available 03/01/2017 5pm EST	Pending
NS13 - Crane Girder Design and Frame Analysis	3/6/2017 7:00:00 PM	Handouts	Available 03/06/2017 5pm EST	Available 03/08/2017 5pm EST	Pending
NS13 - Frame Member and Connection Design	3/13/2017 7:00:00 PM	Handouts	Available 03/13/2017 5pm EST	Available 03/15/2017 5pm EST	Pending
NS13 - Transfer Crane Girder & Longitudinal Brag Bracing Dgn	3/27/2017 7:00:00 PM	Handouts	Available 03/28/2017 5pm EST	Available 03/29/2017 5pm EST	Pending
NS13 - Building Envelope and Bracing Design	4/3/2017 7:00:00 PM	Handouts	Available 04/05/2017 5pm EST	Available 04/05/2017 5pm EST	Pending
NS13 - Final Exam	4/10/2017 7:00:00 PM			Available 04/10/2017 5pm EST	

Night School Resources for 8-session package Registrants

- Weekly “quiz and recording” email.
- Weekly updates of the master Quiz and Attendance record found at www.aisc.org/nightschool. Scroll down to Quiz and Attendance records.
 - Updated on Tuesday mornings.

Night School Resources for 8-session package Registrants

- Webinar connection information:
 - Found in your registration confirmation/receipt.
 - Reminder email sent out Monday mornings.
- Link to handouts also found here.

There's always a solution in steel.

Thank You

Please give us your feedback!
Survey at conclusion of webinar.

