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**Modern Methods for Learning the Basics of Structural Stability: From Behavior to Practice**  
Session 8: Behavior of Structural Systems – Practical Considerations  
December 8, 2020



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Stronger.  
Steel.

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## AISC Live Webinars

### Course Description

Behavior of Structural Systems – Practical Considerations  
December 8, 2020

In this session, the speakers will review the general design for stability requirements provided in the AISC *Specification*. They will discuss the results of the learning module on systems, developing each of the three case studies for a portal frame. They will close out the course with some discussion of how the industry has evolved in its treatment of stability and what the future holds.



## AISC Live Webinars

### Learning Objectives

- Explain how the AISC requirements for stability design are met by the direct analysis method.
- List the analysis methods that are provided in the AISC *Specification* to address stability design.
- Compare the results of an analysis that accounts system geometric imperfections through direct modeling to one that uses notional loads.
- Describe the concept of inelastic design and explain why it may be used more frequently in the future.



## Modern Methods for Learning The Basics of Structural Stability: From Behavior to Practice

Session 8: Behavior of Systems – Practical Considerations  
December 8, 2020



Ronald D. Ziemian, PE, PhD  
Professor  
Bucknell University



Craig Quadrato, PE, PhD  
Associate Principal  
Wiss, Janney, Elstner Associates, Inc.



## Modern Methods for Learning The Basics of Structural Stability: From Behavior to Practice

### Course Introduction

Compression Members

Flexural Members

Beam-Columns

Systems



### Course Overview (2)

Strength/Weight + Stiffness/Weight + Competitive \$

Slender Systems, Members, and Cross-sections

Design for Stability!

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### Course Overview (3)

- Focus of the course is on fundamentals!
- Better understanding of behavior will result in improved design
- Key Definitions
  - **Stability:** Under load, component returns to current state after applying a small disturbance such as a deflection
  - **Bifurcation (critical load):** Theoretical point at which loading a component results in an instantaneous change from current state to significant deflection – two options: not buckled or buckled
  - **Instability:** Loading a component results in a realistic transition from small deflection to significant deflection – buckling preceded by deflection

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### Course Overview (4)

#### "Buckling" Design Methods:

Load

$Load_{lim}$

Bifurcation Theory

Instability Theory

Deflection

Deflection<sub>o</sub>

stiffness ↓  
deflections ↑  
bending ↑

Figure applicable to system, member, and cross-section behavior

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### Course Overview (5)

Analysis acronyms:

**LBA:** linear buckling analysis; **elastic critical load analysis**; elastic eigenvalue analysis; assumes bifurcation theory

**LA:** linear analysis; **1<sup>st</sup>-order elastic analysis**; assumes equilibrium on the undeformed shape and linear elastic material, with no initial imperfections.

**GNA:** geometric nonlinear analysis; **2<sup>nd</sup>-order elastic analysis**; assumes equilibrium on the deformed shape and linear elastic material, with no initial imperfections

**GNIA:** same as GNA, but **includes initial imperfections**

**MNA:** material nonlinear analysis; **1<sup>st</sup>-order inelastic analysis**; assumes equilibrium on the undeformed shape and accounts for yielding, with no initial imperfections

**GMNIA:** geometric and material nonlinear analysis; **2<sup>nd</sup>-order inelastic analysis**; assumes equilibrium on the deformed shape, accounts for yielding, and includes initial imperfections

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### Modern Methods for Learning The Basics of Structural Stability: From Behavior to Practice

Course Introduction

Compression Members – Sessions 1 & 2

Flexural Members – Session 3 & 4

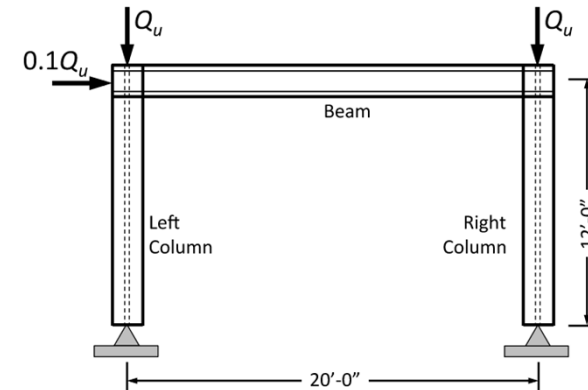
Beam-Columns – Sessions 5 & 6

Systems – Session 7 & 8



### Session 8

System Behavior Lab



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### Session Overview

- Review Direct Analysis Method
- Perform LM9
- Looking to the Future by Starting with the Past with Ron



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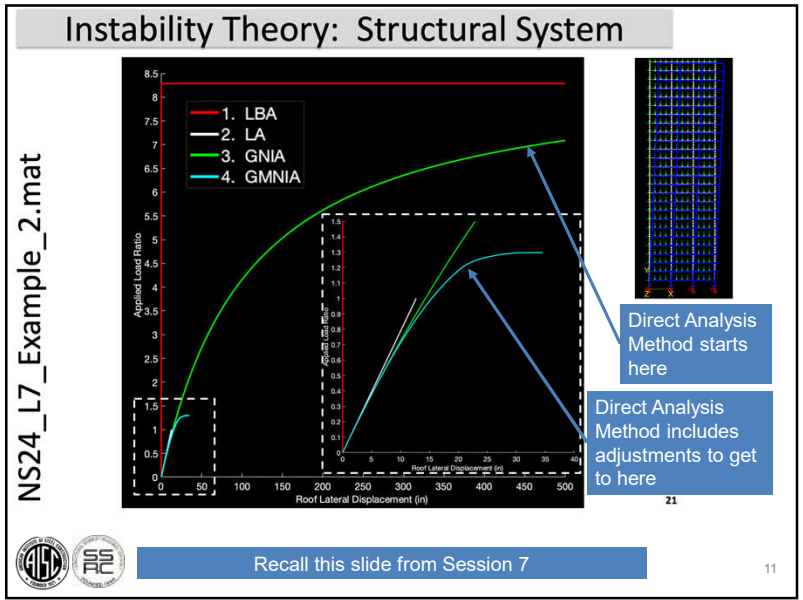
### Session 7 in AISC 360-16 General Stability Requirements (C1)

- Member stability must account for:
  - Axial, flexural, shear, torsional, connection deformations
  - Second order effects (P- $\Delta$  and P- $\delta$ )
  - Geometric imperfection
  - Stiffness reductions due to inelasticity
  - Uncertainty in system, member, and connection strength and stiffness

Session 5  
Slide 82  
&  
Chapter C



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## Session 7 in AISC 360-16 Direct Analysis Method

Basic Requirement in Section C1	Provision in Direct Analysis Method (DM)	Provision in Effective Length Method (ELM)
(1) Consider all deformations	C2.1(a). Consider all deformations	Same as DM (by reference to C2.1)
(2) Consider second-order effects (both P <sub>1</sub> and P <sub>2</sub> )	C2.1(b). Consider second-order effects (P <sub>1</sub> s and P <sub>2</sub> s)	Same as DM (by reference to C2.1)
(3) Consider geometric imperfections. This includes joint-position imperfections <sup>(a)</sup> (which affect structure response) and member imperfections (which affect structure response and member strength)	C2.2a. Direct modeling of C2.2b. Notional loads Effect of system imperfections on structure response Effect of member imperfections on structure response Effect of member imperfections on member strength	Same as DM, second order only (by reference to C2.2b) All these effects are considered by using L <sub>e</sub> = KL from a side-sway buckling analysis in the member strength check. Note that the differences between DM and ELM are: • DM uses reduced stiffness in the member strength check and L <sub>e</sub> = L in the member strength check • ELM uses full stiffness in the analysis and L <sub>e</sub> = KL from side-sway buckling analysis in the member strength check
(4) Consider stiffness reduction due to inelasticity. This affects structure response and member strength	Effect of stiffness reduction on structure response Effect of stiffness reduction on member strength	Included in the stiffness reduction specified in C2.3 Included in member strength formulas, with L <sub>e</sub> = L
(5) Consider uncertainty in strength and stiffness. This affects structure response and member strength	Effect of stiffness/strength uncertainty on structure response Effect of stiffness/strength uncertainty on member strength	Included in the stiffness reduction specified in C2.3 Included in member strength formulas, with L <sub>e</sub> = L

Big 5

Basic Requirements must be considered, but to what degree is based on Engineer's judgement

Note that stiffness reduction and member strength formulas account for multiple requirements

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## Session 7 in AISC 360-16 Direct Analysis Method

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Deflected Shape: 2<sup>nd</sup>-Order Elastic, Incr # 20, Applied Load Ratio = 1

Accomplished via Computational Analysis (GNA)

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## Session 7 in AISC 360-16 Direct Analysis Method

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Deflected Shape: 2<sup>nd</sup>-Order Elastic, Incr # 20, Applied Load Ratio = 1

$N_i = 0.002\alpha Y_i$  (C2-1)  
 where  
 $\alpha = 1.0$  (LRFD);  $\alpha = 1.6$  (ASD)  
 $N_i$  = notional load applied at level  $i$ , kips (N)  
 $Y_i$  = gravity load applied at level  $i$  from the LRFD load combination or ASD load combination, as applicable, kips (N)

Accomplished via Computational Analysis (GNIA with imperfections modelled directly or with notional loads)

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## Session 7 in AISC 360-16 Direct Analysis Method

- 0.8 factor applied to all stiffnesses contributing to structure stability

**TABLE C-C1.1  
Comparison of Basic Stability Requirements with Specific Provisions**

Basic Requirement in Section C1	Provision in Direct Analysis Method (DM)	Provision in Effective Length Method (ELM)
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(a) In typical building structures, the "joint-rotation imperfections" refers to column out-of-plumbness.  
(b) Second-order effects may be considered either by a computational P-Δ and P-δ analysis or by the approximate method (using (a) and (b) multiples) specified in Appendix 8.



## Session 7 in AISC 360-16 Direct Analysis Method

- 0.8 factor applied to all stiffnesses contributing to structure stability
- Additional  $\tau_b$  on flexural stiffness of members whose flexural stiffness contribute to stability if  $\alpha P_r/P_{ns} > 0.5$
- If  $\alpha P_r/P_{ns} > 0.5$  additional  $0.001\alpha Y_1$  may be used in lieu of  $\tau_b$

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## Session 7 in AISC 360-16 Direct Analysis Method

The nominal compressive strength,  $P_n$ , shall be determined based on the limit state of flexural buckling:

$$P_n = F_c A_g \quad (E3-1)$$

The critical stress,  $F_c$ , is determined as follows:

(a) When  $\frac{L_c}{r} \leq 4.71 \sqrt{\frac{E}{F_y}}$  (or  $\frac{F_c}{F_y} \leq 2.25$ )

$$F_c = \left( 0.658 \frac{F_y}{F_c} \right) F_y \quad (E3-2)$$

(b) When  $\frac{L_c}{r} > 4.71 \sqrt{\frac{E}{F_y}}$  (or  $\frac{F_c}{F_y} > 2.25$ )

$$F_c = 0.877 F_y \quad (E3-3)$$

where  
 $A_g$  = gross cross-sectional area of member, in<sup>2</sup> (mm<sup>2</sup>)  
 $E$  = modulus of elasticity of steel = 29,000 ksi (200,000 MPa)

E3 shown, see E4 for torsional and flexural-torsional buckling

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(b) Second-order effects may be considered either by a computational P-Δ and P-δ analysis or by the approximate method (using (a) and (b) multiples) specified in Appendix 8.



## Direct Analysis Method

- Stiffness reductions account for the following on structural response
  - Axial, flexural, shear, torsional, connection deformations
  - Second order effects (P-Δ and P-δ)
  - Geometric imperfection
  - Inelasticity
  - Uncertainty

(a) When  $\frac{P_r}{P_c} \geq 0.2$

$$\frac{P_r}{P_c} \leq \frac{8}{9} \left( \frac{M_{rx} + M_{ry}}{M_{cx} + M_{cy}} \right) \leq 1.0 \quad (H1-1a)$$

(b) When  $\frac{P_r}{P_c} < 0.2$

$$\frac{P_r}{2P_c} + \left( \frac{M_{rx} + M_{ry}}{M_{cx} + M_{cy}} \right) \leq 1.0 \quad (H1-1b)$$

- Member strength formulas account for the following on member strength
  - Member imperfections (Axial Only)
  - Inelasticity
  - Uncertainty



## Session 7 in AISC 360-16

- Other Stability Design Methods
  - Effective length (Appendix 7)
  - First-order analysis (Appendix 7)
  - Advanced analysis (Appendix 1)
    - Elastic
    - Inelastic
- Alternative analysis method: Approximate second-order analysis (Appendix 8)



Larry Griffis  
Don White

$$M_r = B_1 M_{nt} + B_2 M_{lt} \quad (A-8-1)$$

$$P_r = P_{nt} + B_2 P_{lt} \quad (A-8-2)$$



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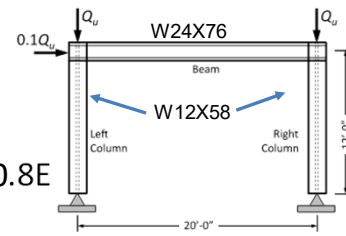
## Learning Module 9 Objectives

- Apply the Direct Analysis Method to assess structural system adequacy
- Use rigorous second-order analysis to determine beam-column required strength
- Use notional loads to simulate initial imperfections and stiffness reduction due to partial yielding
- Use interaction equations to check member adequacy
- Use drift ratios as indicator of system sensitivity to second-order effects

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## Learning Module 9 Method

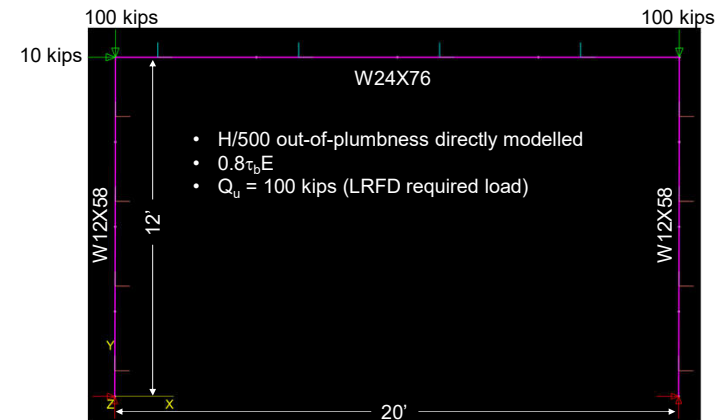
- A992 STEEL
- Beam  $L_b = L_c = 0$
- Stiffness reduction of 0.8E
- Three studies
  - Case 1: H/500 out-of-plumbness &  $\tau_b$
  - Case 2: Use Case 1 to find  $Q_u$  for DCR = 1.0
  - Case 3: Use notional loads instead of out-of-plumbness and  $\tau_b$



LRFD Methodology

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## Learning Module 9 Case 1 Model



Use Direct Analysis Method

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## Learning Module 9 Member Capacities ( $P_c$ and $M_c$ )

- W12x58 Left Column
  - $P_c = \phi P_n = 603$  kips
  - $M_c = \phi M_{ny} = 1464$  kip-in
- W12x58 Right Column
  - $P_c = \phi P_n = 603$  kips
  - $M_c = \phi M_{ny} = 1464$  kip-in

Note in this study  $\phi$  factors are included



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## Learning Module 9 Member Capacities ( $P_c$ and $M_c$ )

- W24x76 Beam
- $P_c = \phi P_n = 1008$  kips
- $M_c = \phi M_p = 9000$  kip-in

Note in this study  $\phi$  factors are included



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First, let's check how sensitive this system is to 2<sup>nd</sup> order effects using the Direct Analysis Method

### Stability Sensitive Structural Systems

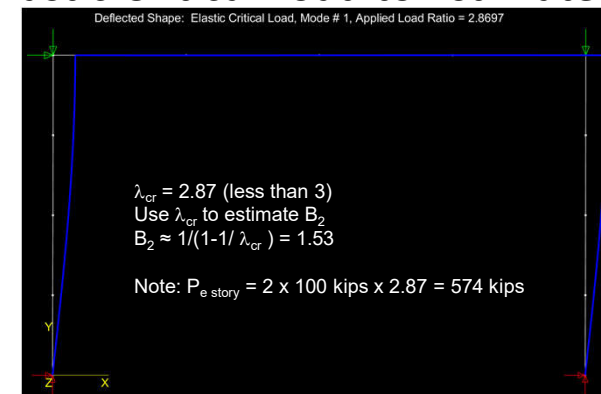
- Indicators include:
  - $B_1$  and  $B_2$  factors
  - Elastic/Inelastic critical buckling load factors  $\lambda_{cr}$  and mode shapes
  - Natural periods and mode shapes
- Eurocode uses ratio  $\lambda_{cr}$  (think LBA) between the the critical buckling loading and applied loading :
  - $\lambda_{cr} < 3$ , must employ rigorous 2<sup>nd</sup>-order analysis ( $B_2 > 1.5$ )
  - $3 \leq \lambda_{cr} < 10$ , approximate methods acceptable
  - $\lambda_{cr} \geq 10$ , no need to consider P- $\Delta$  effects ( $B_2 < 1.1$ )



Recall this slide from Session 7

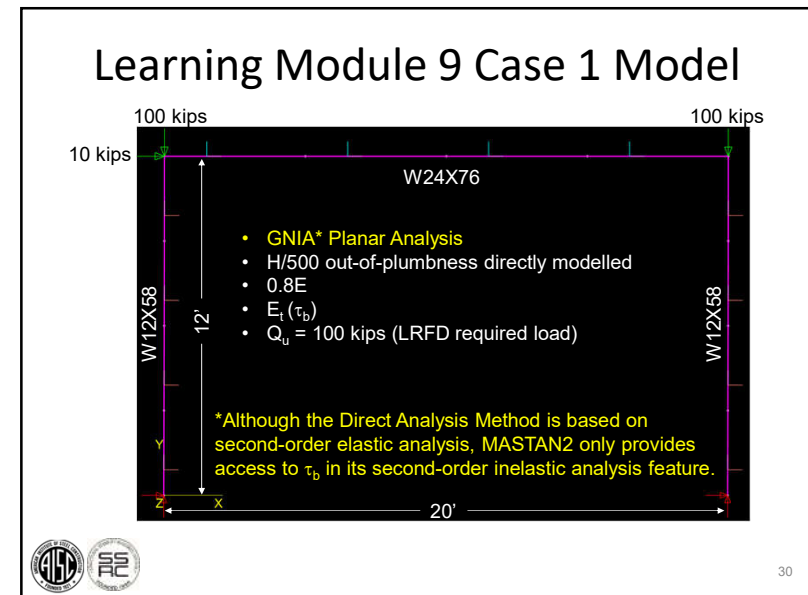
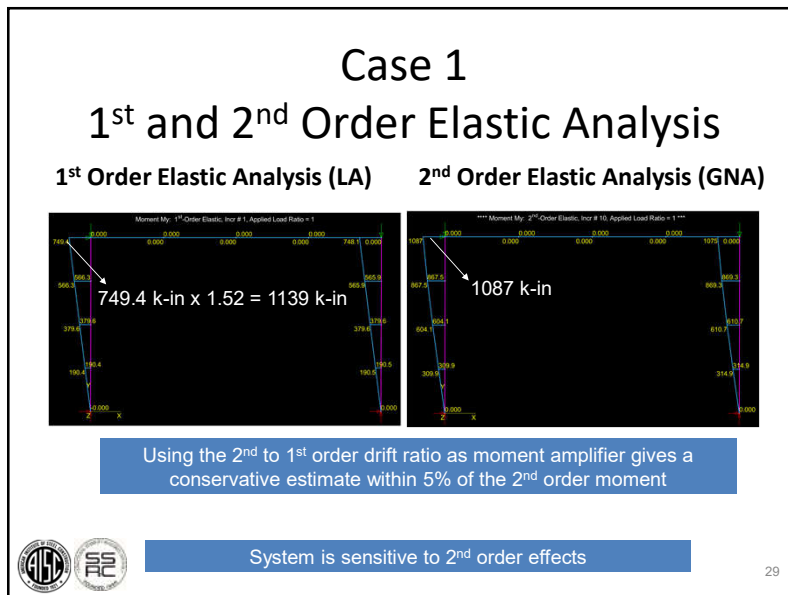
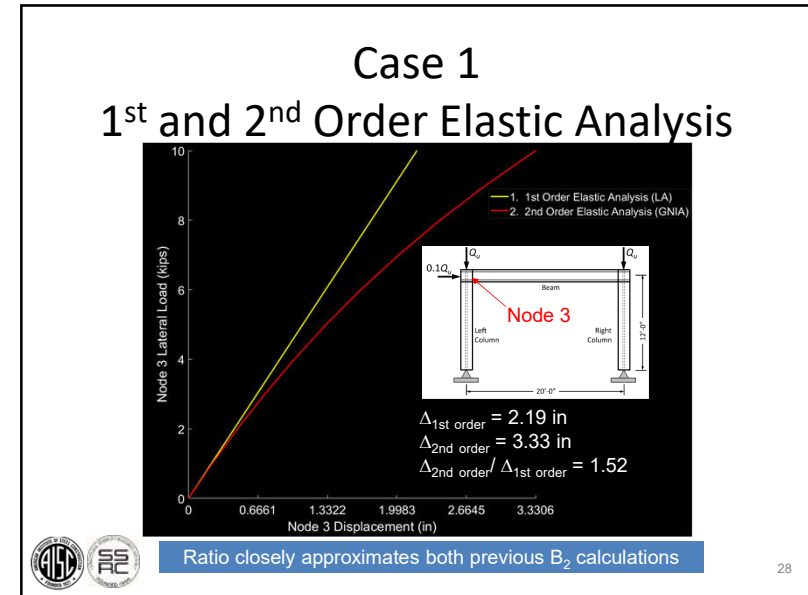
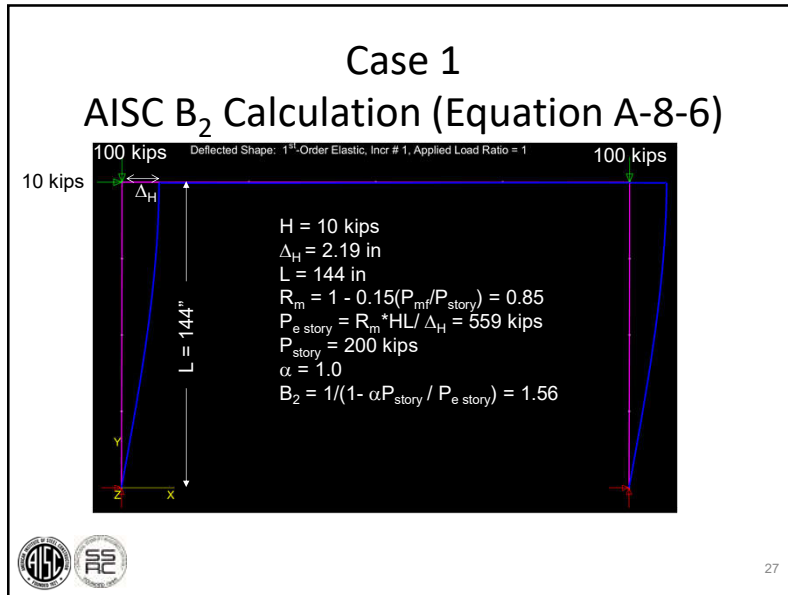
25

## Case 1 Elastic Critical Load to Estimate $B_2$



System is sensitive to 2<sup>nd</sup> order effects

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### Case 1 Interaction Values W12x58 Left Column

(a) When  $\frac{P_r}{P_c} \geq 0.2$

$$\frac{P_r}{P_c} + \frac{8}{9} \left( \frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \right) \leq 1.0 \quad \text{(H1-1a)}$$

(b) When  $\frac{P_r}{P_c} < 0.2$   $0.15$

$$\frac{P_r}{2P_c} + \left( \frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \right) \leq 1.0 \quad 0.82 \quad \text{(H1-1b)}$$

91 kips
1087 kip-in  
603 kips
1464 kip-in  
1206 kips
1464 kip-in



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### Case 1 Interaction Values W12x58 Right Column

(a) When  $\frac{P_r}{P_c} \geq 0.2$

$$\frac{P_r}{P_c} + \frac{8}{9} \left( \frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \right) \leq 1.0 \quad \text{(H1-1a)}$$

(b) When  $\frac{P_r}{P_c} < 0.2$   $0.18$

$$\frac{P_r}{2P_c} + \left( \frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \right) \leq 1.0 \quad 0.83 \quad \text{(H1-1b)}$$

109 kips
1076 kip-in  
603 kips
1464 kip-in  
1206 kips
1464 kip-in



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### Case 1 Interaction Values W24x76 Beam

(a) When  $\frac{P_r}{P_c} \geq 0.2$

$$\frac{P_r}{P_c} + \frac{8}{9} \left( \frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \right) \leq 1.0 \quad \text{(H1-1a)}$$

(b) When  $\frac{P_r}{P_c} < 0.2$   $0.005$

$$\frac{P_r}{2P_c} + \left( \frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \right) \leq 1.0 \quad 0.12 \quad \text{(H1-1b)}$$

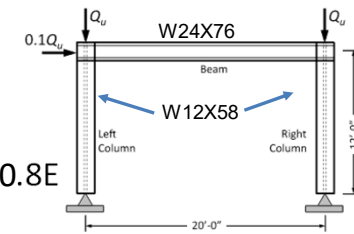
4.7 kips
1087 kip-in  
1008 kips
9000 kip-in  
2016 kips
9000 kip-in



37

### Learning Module 9 Method

- A992 STEEL
- Beam  $L_b = L_c = 0$
- Stiffness reduction of 0.8E
- Three studies
  - Case 1: H/500 out-of-plumbness &  $\tau_b$
  - Case 2: Use Case 1 to find  $Q_u$  for DCR = 1.0
  - Case 3: Use notional loads instead of out-of-plumbness and  $\tau_b$



LRFD Methodology

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### Case 2 Take 1 Interaction Values W12x58 Right Column

When  $\frac{P_r^*}{P_c} \geq 0.2$  **0.22**

132 kips  
603 kips

132 kips  
603 kips

1423 kip-in  
1464 kip-in

**CASE 2 TAKE 1**  
 $\frac{P_r^*}{P_c} + \frac{8}{9} \left( \frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \right) \leq 1.0$  **1.08**  $Q_u = 120$  kips (HI-1a)

When  $\frac{P_r^*}{P_c} < 0.2$  **0.18**


109 kips  
603 kips

109 kips  
1206 kips

1076 kip-in  
1464 kip-in

**CASE 1**  
 $\frac{P_r^*}{2P_c} + \left( \frac{M_{rx}}{M_{cx}} + \frac{M_{ry}}{M_{cy}} \right) \leq 1.0$  **0.83**  $Q_u = 100$  kips (HI-1b)

Try about 2/3 of the way between two for  $Q_u = 114$  kips



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### Learning Module 9 Case 2 Take 2 Model

$Q_u = 114$  kips  $Q_u = 114$  kips

$0.1Q_u = 11.4$  kips

W24X76


12'

20'

W12X58

- GNIA Planar Analysis
- H/500 out-of-plumbess directly modelled
- 0.8E
- $E_t(\tau_b)$
- Take 2:  $Q_u = 114$  kips

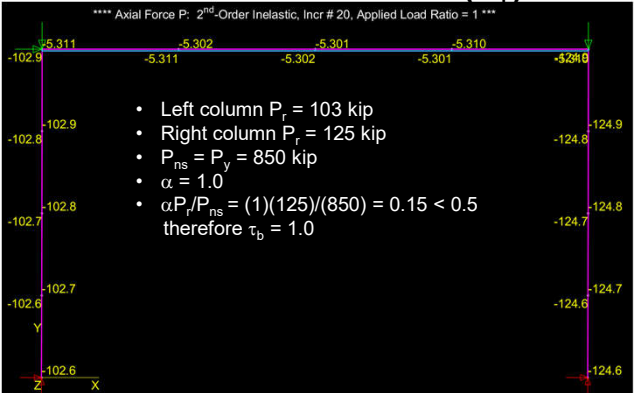
Model NS24\_L8\_Example\_2



44


### Case 2 Take 2 Axial Load Effects ( $P_r$ )

\*\*\*\* Axial Force P: 2<sup>nd</sup>-Order Inelastic, Incr # 20, Applied Load Ratio = 1 \*\*\*\*



- Left column  $P_r = 103$  kip
- Right column  $P_r = 125$  kip
- $P_{ns} = P_y = 850$  kip
- $\alpha = 1.0$
- $\alpha P_r / P_{ns} = (1)(125)/(850) = 0.15 < 0.5$   
therefore  $\tau_b = 1.0$

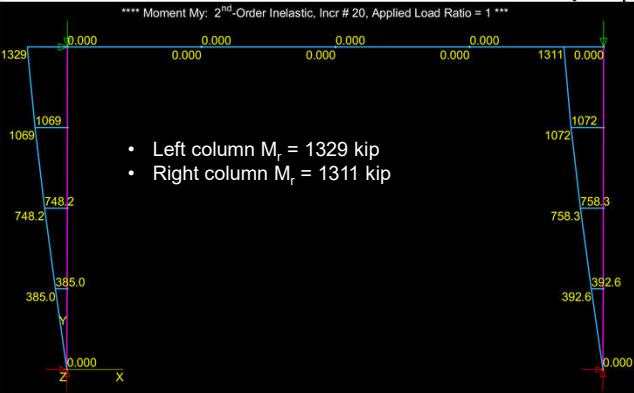
Model NS24\_L8\_Example\_2



45


### Case 2 Take 2 Column Flexural Load Effects ( $M_r$ )

\*\*\*\* Moment My: 2<sup>nd</sup>-Order Inelastic, Incr # 20, Applied Load Ratio = 1 \*\*\*\*



- Left column  $M_r = 1329$  kip
- Right column  $M_r = 1311$  kip

Model NS24\_L8\_Example\_2



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## Case 2 Take 2 Interaction Values W12x58 Right Column

125 kips  
When  $\frac{P_r^*}{P_{ca}} \geq 0.2$  0.21  
603 kips  $\frac{P_r^*}{P_{ca}} + \frac{8}{9} \left( \frac{M_{rx}^*}{M_{cx}} + \frac{M_{ry}^*}{M_{cy}} \right) \leq 1.0$  1.00  $Q_u = 114$  kips (HI-1a)

132 kips  
When  $\frac{P_r^*}{P_{ca}} \geq 0.2$  0.22  
603 kips  $\frac{P_r^*}{P_{ca}} + \frac{8}{9} \left( \frac{M_{rx}^*}{M_{cx}} + \frac{M_{ry}^*}{M_{cy}} \right) \leq 1.0$  1.08  $Q_u = 120$  kips (HI-1a)

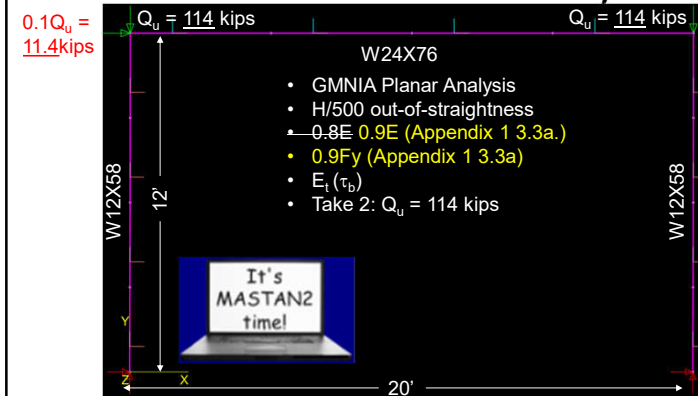
109 kips  
When  $\frac{P_r^*}{P_{ca}} < 0.2$  0.18  
603 kips  $\frac{P_r^*}{2P_{ca}} + \left( \frac{M_{rx}^*}{M_{cx}} + \frac{M_{ry}^*}{M_{cy}} \right) \leq 1.0$  0.83  $Q_u = 100$  kips (HI-1b)

1311 kip-in CASE 2 TAKE 2  
1464 kip-in  
1423 kip-in CASE 2 TAKE 1  
1464 kip-in  
1076 kip-in CASE 1  
1206 kips 1464 kip-in



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## Case 2 Take 2 2<sup>nd</sup> Order Inelastic Analysis



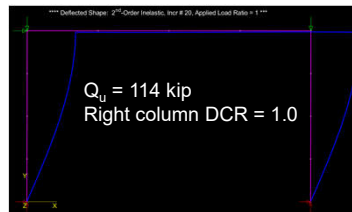
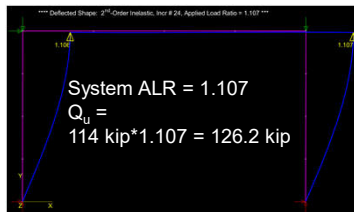
Model NS24\_L8\_Example\_3

48

## Case 2 Take 2 Inelastic Analysis vs Direct Analysis Method

Direct Analysis Method-GMNIA  
(Appendix 1.3)

Direct Analysis Method-GNIA  
(Chapter C)

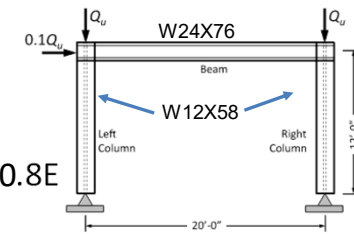


Model NS24\_L8\_Example\_3

49

## Learning Module 9 Method

- A992 STEEL
- Beam  $L_b = L_c = 0$
- Stiffness reduction of 0.8E
- Three studies



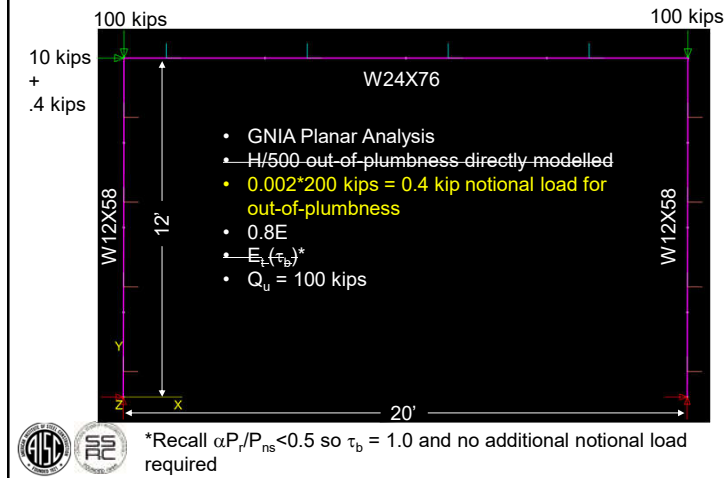
- Case 1: H/500 out-of-plumbness &  $\tau_b$
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- Case 3: Use notional loads instead of out-of-plumbness and  $\tau_b$



LRFD Methodology

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## Learning Module 9 Case 3 Model



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## Learning Module 9 Case 3

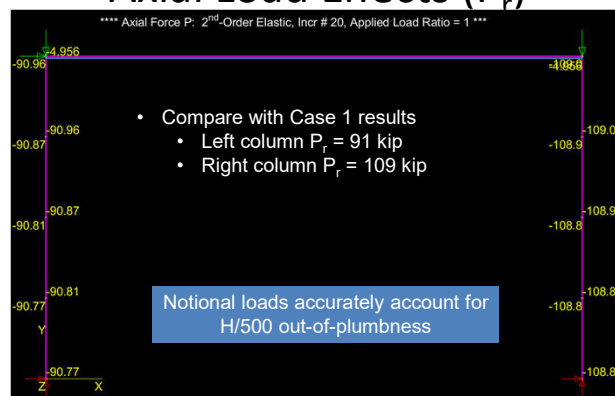
General Stability Requirement	How Accomplished
Deformations	GNIA via MASTAN2
Second order effects	GNIA via MASTAN2
System imperfections on structure	Notional Load ( $0.002 \Sigma Q_u$ )
Member imperfections on structure	$0.8E$ via MASTAN2
Member imperfections on member strength	$P_c$
Stiffness reductions due to inelasticity on structure	$0.8E$ via MASTAN2
Stiffness reductions due to inelasticity on member strength	$P_c$
Uncertainty on structure	$0.8E$ via MASTAN2
Uncertainty on member	$P_c$



Model NS24\_L8\_Example\_4

52

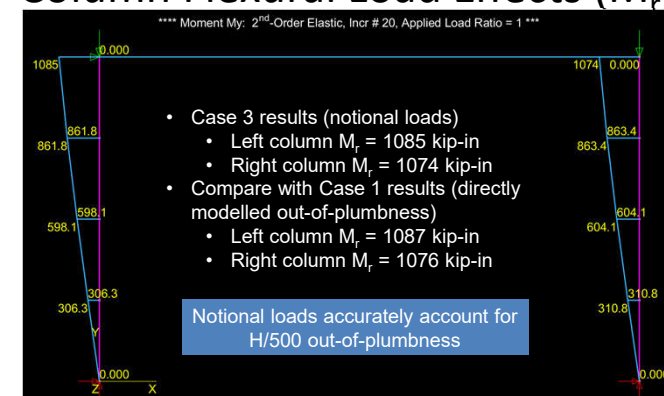
## Case 3 Axial Load Effects ( $P_r$ )



Model NS24\_L8\_Example\_4

53

## Case 3 Column Flexural Load Effects ( $M_r$ )



Model NS24\_L8\_Example\_4

54

## Summary

- General stability requirements “the BIG 5” must be considered
- The Direct Analysis Method in Chapter C is based on a second order elastic analysis and is one way to account for general stability requirements
- There are 4 other AISC stability design methods in Appendices 1 and 7 that can be used to account for the general stability requirements

And now heeeeeeeeeeeeeee's Ronny!



55

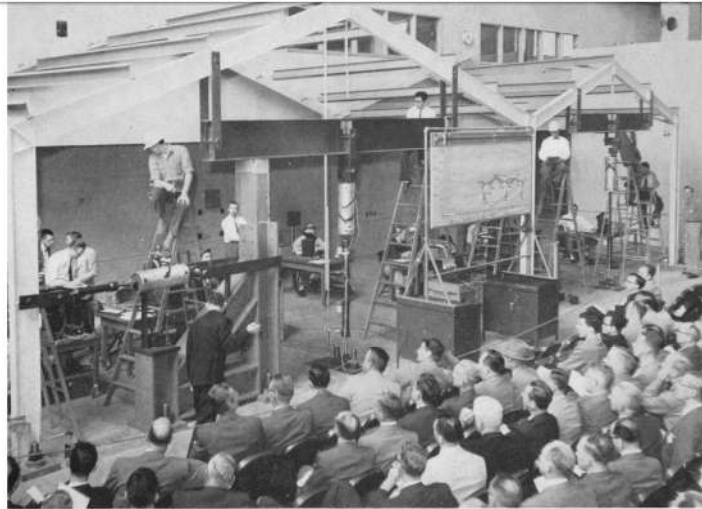


Design and analysis, perfect together...

**LOOKING TO THE FUTURE BY  
STARTING WITH THE PAST...**

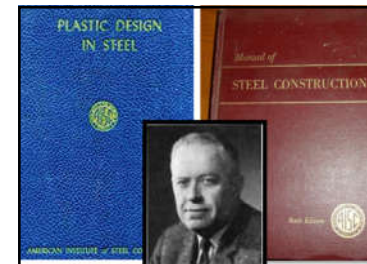
56

## Thoughts on future of advanced analysis in design...



Fifty-foot Two-span Continuous Gabled Frame Test at Lehigh University

57



## AISC, 6<sup>th</sup> Edition PART 2

### SECTION 2.1 SCOPE (ADOPTED NOVEMBER 30, 1961)

Subject to the limitations contained herein, simple or continuous beams, one and two-story rigid frames classified as Type 1 construction in Sect. 1.2 and similar portions of structures rigidly constructed so as to be continuous over at least one interior support,\* may be proportioned on the basis of plastic design, i.e., of their maximum strength. This strength, as determined by rational analysis, shall not be less than that required to support 1.70 times the given live load and dead load for simple and continuous beams. For continuous frames it shall not be less than 1.85 times the given live load and dead load, nor 1.40 times these loads acting in conjunction with 1.40 times any specified wind or earthquake forces.

58



Plastic Design of a 14-Story Apartment Building  
WILLIAM A. BENNETT  
AISC ENGINEERING JOURNAL  
APRIL / 1967

**Bennett indicates...Better understanding of stability and strength limit state behavior resulted in a better design**

- ✓ More rational method
- ✓ Significant economies gained
- ✓ Included P-Δ effects
- ✓ Track limit state behavior
- ✓ More flexibility in design process

“It is expected that further research will produce computer programs which can provide solutions for extremely complex frames and include more secondary effects, as well as proportional and nonproportional loading of frames.”

*Plastic Design in Steel - Guide and Commentary*  
ASCE, 1971



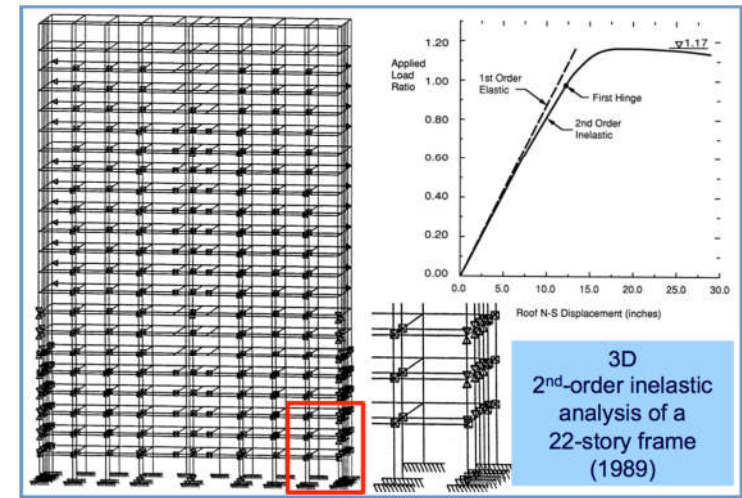
Computer programs -  
lots of further research...

1970's

- Computing hardware
- Graphical user interfaces
- Geometric nonlinear:
  - 2<sup>nd</sup>-order effects ( $P-\Delta$ ,  $P-\delta$ )
- Material nonlinear:
  - Plastic hinge vs. zone

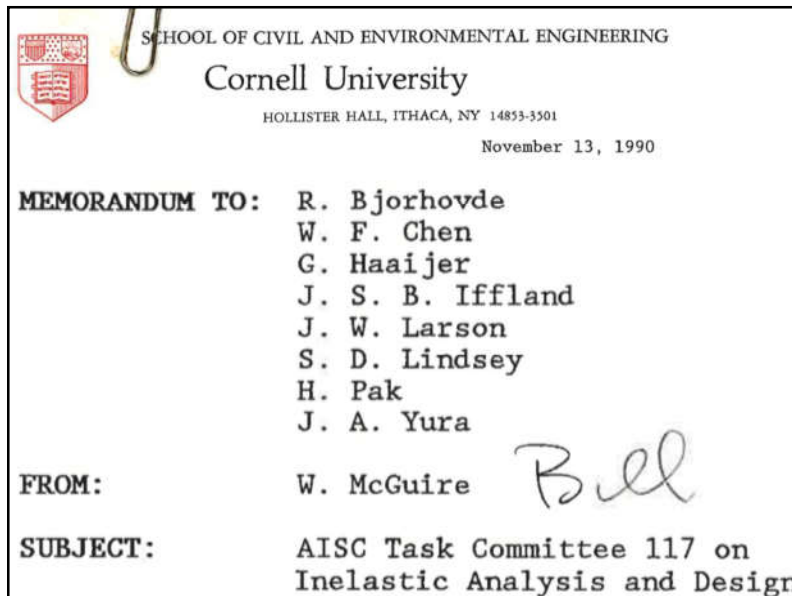
1990's

63



3D  
2<sup>nd</sup>-order inelastic  
analysis of a  
22-story frame  
(1989)

64



Computer programs -  
lots of further research...

1970's

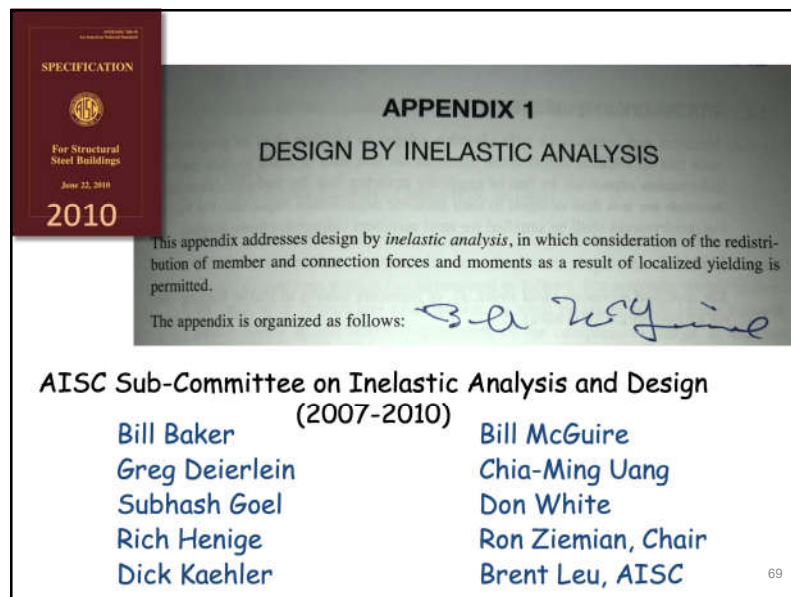
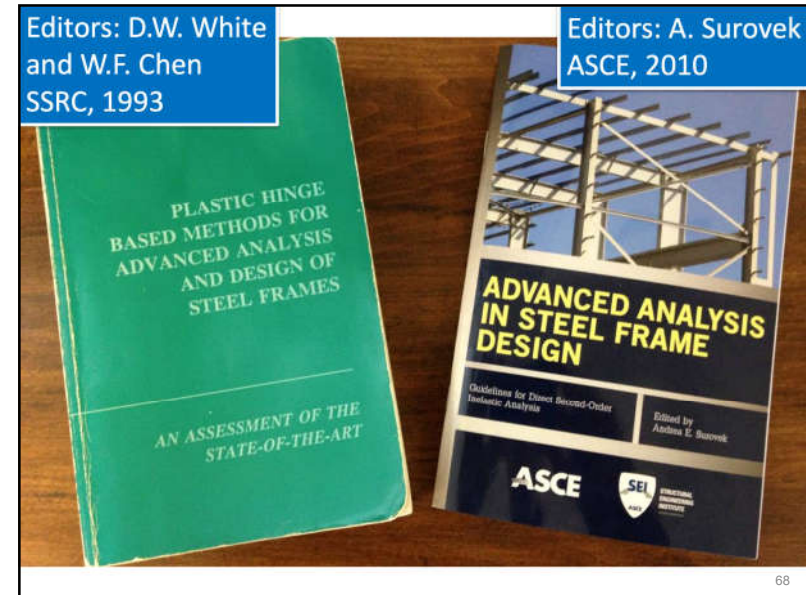
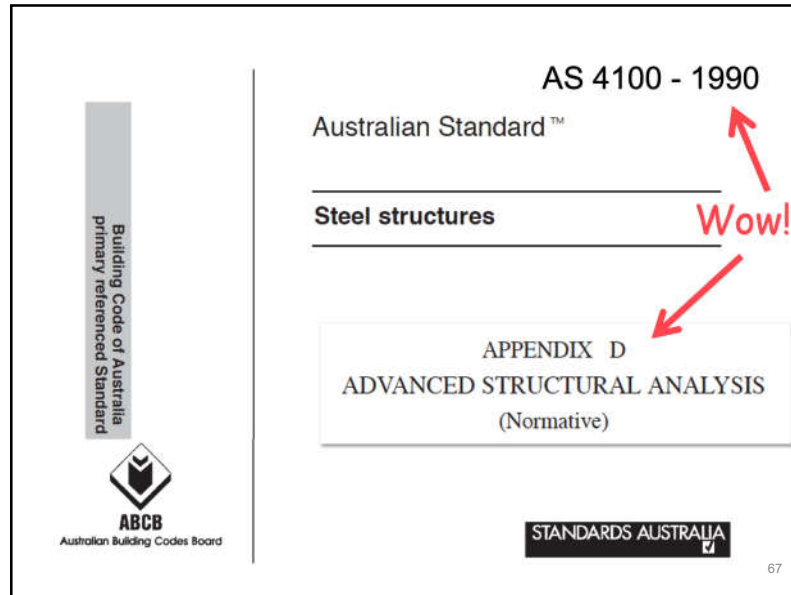
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  - Plastic hinge vs. zone

1990's



U.S. steel design profession  
slow to adopt limit states  
design philosophy (LRFD)

66



### Inelastic analysis and seismic design, perfect together...

- Over the years, the use of pushover analyses has become quite common, especially for structures in high seismic areas
- Today, the use of full nonlinear, or at least material nonlinear, time history analyses are now sometimes being employed
- With this in mind, AISC has recently formed an ad hoc TG on Seismic Analysis (John Hooper – Chair)
  - Direct Analysis Method dovetail with seismic
  - AISC 341 may include a new Appendix 1 - Design Verification Using Nonlinear Response History Analysis

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71

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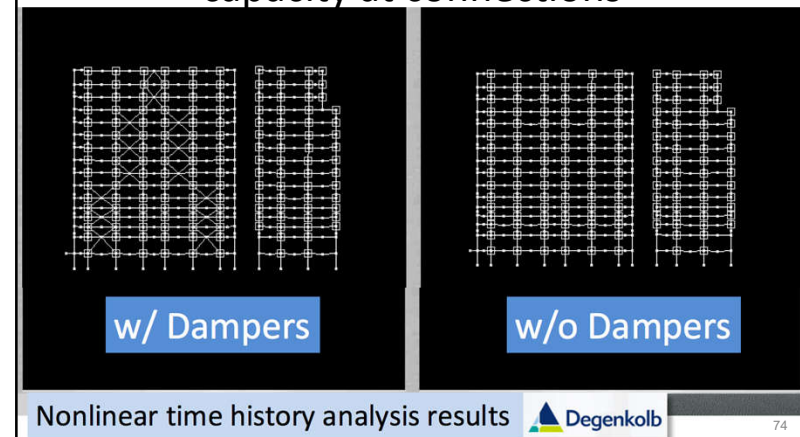
72

## Caltrans District 4 Office Building retrofitted with viscous dampers (Oakland, CA)

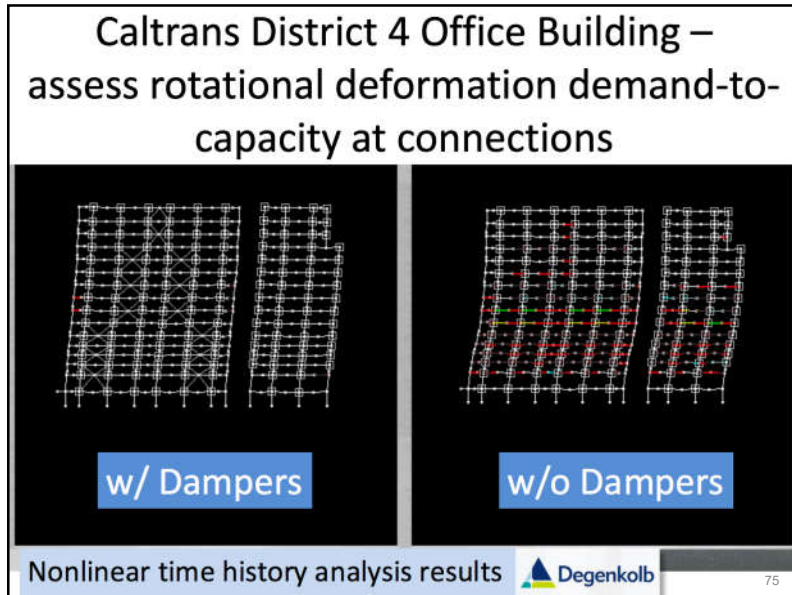


73

## Caltrans District 4 Office Building – assess rotational deformation demand-to- capacity at connections



74



### Future of Advanced Analysis in Design

- Focus will shift to better modeling the load effects...Dynamic loading due to Earth, Wind, & Fire
- Future speeds of computer hardware/software will permit amazingly sophisticated nonlinear time history analyses...yeah!
- But...if we could suddenly increase the speed of our computers by 1,000x, would the SE profession?
  - a) Use existing analysis capabilities, but quadruple the number of load cases currently being investigated
  - b) Continue to investigate the same number of load cases, but perform much more sophisticated analyses of many of them
- Virtual reality, artificial intelligence, and big data? 76

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- Virtual reality, artificial intelligence, and big data? <sup>79</sup>

### Fundamentals!

Intuition

Education

Codes, Specifications, Design Guides

Computational Analysis

Experience = you + colleagues

### Structural Stability

Guide (not replace) your judgement

80

### Happy Holidays!

Victor Gomes and Professor Luiz Vieira  
University of Campinas  
São Paulo, Brazil

Material # 1

Success: Material attached

### With warmest wishes, Ron and Craig

### Thank You!

Hope you enjoyed this lecture!

Smarter. Stronger. Steel.

## Single-Session Registrants

### CEU / PDH Certificates

- You will receive an email on how to report attendance from: [registration@aisc.org](mailto:registration@aisc.org).
- Be on the lookout: Check your spam filter! Check your junk folder!
- Completely fill out online form. Don't forget to check the boxes next to each attendee's name!



## Single-Session Registrants

### CEU / PDH Certificates

- Reporting site (URL will be provided in the forthcoming email).
- Username: Same as AISC website username.
- Password: Same as AISC website password.



## 8-Session Registrants

### CEU / PDH Certificates

One certificate will be issued at the conclusion of the course.



## 8-Session Registrants

### Attendance and PDH Certificates

- You have two options to receive credit for a given session.
  - Option 1: Watch the live session. Credit for live attendance will be displayed on the Course Resources table within two days of the session.
  - Option 2: Watch the recording and pass the associated quiz.

### Videos and Quizzes

- For each session, find access within two business days after the live air date. (An email will be sent from [nightschool@aisc.org](mailto:nightschool@aisc.org).)
- Reasons for quiz:
  - EEU – You must take all quizzes and the final exam to receive EEU.
  - PDHs – If you watch a recorded session, you must pass quiz for PDHs.
  - Reinforce what you learn in the lectures and get more out of the course!

### Distribution of Certificates

All certificates will be issued after the course is completed. Only the registrant will receive a certificate for the course.



## 8-Session Registrants

### Course Resources

Find all your handouts, quizzes and quiz scores, recording access, and attendance information in one place!



## 8-Session Registrants

### Course Resources

Go to [www.aisc.org](http://www.aisc.org) and sign in.

## 8-Session Registrants

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## 8-Session Registrants


### Course Resources

Event	Start Date
Session Design in Steel	1/12/2020 12:00:00 AM
8-Session Package Design of Fabric Attachments	5/9/2018 1:00:00 PM
MS 13 8-Session Package Night School 13 - Fundamentals of Connection Design	10/1/2017 7:00:00 PM
MS 16 8-Session Package Night School 16 - Seismic Design in Steel	2/9/2018 7:00:00 PM
MS 17 8-Session Package Night School 17 - Design of Fabric Attachments	7/23/2018 7:00:00 PM
MS 18 8-Session Package Night School 18 - Steel Construction: 16 1/2 Trainers Day	10/1/2018 7:00:00 PM
MS 19 8-Session Package Night School 19 - Connection Design	2/4/2019 7:00:00 PM
MS 20 8-Session Package Night School 20 - Clinical Methods of Structural Analysis	6/29/2019 7:00:00 PM
8-Session Package Seismic Design in Steel - Concrete & Reinforce	7/30/2018 1:00:00 PM




## 8-Session Registrants

### Course Resources



EDUCATION | PUBLICATIONS | AWARDS AND COMPETITIONS | TECHNICAL RESOURCES | STEEL SOLUTIONS CENTER



AISC | MY ACCOUNT > COURSE RESOURCES > NS24 8-SESSION PACKAGE RESOURCES

#### Night School 24: Modern Methods for Learning Structural Stability

##### 8-SESSION PACKAGE RESOURCES

Event	Date	Webinars	Video	Quiz	Attendance
NS24.1 - Compression Members - The Fundamentals	Oct 6, 2020 7:00PM EDT	Completed	Available 10/06/2020 5:00PM EDT	Available 10/06/2020 5:00PM EDT	Pending
NS24.2 - Compression Members - Practical Considerations	Oct 13, 2020 7:00PM EDT	Completed	Available 10/13/2020 5:00PM EDT	Available 10/13/2020 5:00PM EDT	Pending
NS24.3 - Behavior of Tension Members - The Fundamentals	Oct 20, 2020 7:00PM EDT	Completed	Available 10/20/2020 5:00PM EDT	Available 10/20/2020 5:00PM EDT	Pending
NS24.4 - Tension Members - Practical Considerations	Oct 27, 2020 7:00PM EDT	Completed	Available 10/27/2020 5:00PM EDT	Available 10/27/2020 5:00PM EDT	Pending
NS24.5 - Stability of Beam-Columns - The Fundamentals	Nov 3, 2020 7:00PM EDT	Completed	Available 11/03/2020 5:00PM EDT	No longer available	Pending
NS24.6 - Stability of Beam-Columns - Practical Considerations	Nov 10, 2020 7:00PM EDT	Completed	Available 11/10/2020 5:00PM EDT	No longer available	Pending
NS24.7 - Behavior of Structural Systems - The Fundamentals	Dec 1, 2020 7:00PM EDT	Completed	Available 12/01/2020 5:00PM EDT	No longer available	Pending
NS24.8 - Structural Systems - Practical Considerations	Dec 8, 2020 7:00PM EDT	Completed	Available 12/08/2020 5:00PM EDT	No longer available	Pending
NS24 - Final Exam	N/A			No longer available	



AISC | Thank you.




Smarter.  
Stronger.  
Steel.